

ECEn 370

Homework Problem Set 10

Due on Friday, March 16, 2011.

From Bertsekas and Tsitsiklis, *Introduction to Probability, 2nd Ed.*

1. Chapter 4 Problem 29
2. Chapter 4 Problem 30
3. Chapter 4 problem 31
4. Chapter 4 Problem 33
5. Chapter 4 Problem 35
6. Chapter 4 Problem 36
7. Chapter 4 Problem 41
8. Chapter 4 Problem 43
9. Chapter 4 Problem 44
10. MATLAB Problem

Sum of a Binomial Number of Independent Uniform Random Variables

Suppose you live in a small town of a hundred people and you own a small store. Every normal day (excluding Sundays of course) each person in the town has the probability $p = 0.25$ of visiting your store. A person that visits your store will spend money distributed uniformly from 0 to 50 dollars. The amount of money spent in your store on any normal day is Y .

- a) Analytically compute the following: mean of Y , standard deviation of Y (consider page 242 in the book).
- b) Simulate this problem in the following fashion (turn in your code):
Do the following loop 10,000 times
 - Generate the number of people, n , that visit your store every day by a Binomial random variable.
 - Sum together n random variables with uniform distributions from 0 to 50.
 - Store the sum of money - this is one outcome of the random variable Y .After the loop is complete, then compute the mean and standard deviation of the outcomes for Y .
- c) Plot a histogram representing the pdf of Y .
- d) Do the simulated values you computed in part b) match the values in part a)?