

**ECEn 370**

**Homework Problem Set 10**

Due on Wednesday, March 19, 2014.

From Bertsekas and Tsitsiklis, *Introduction to Probability, 2nd Ed.*

1. (5 pts) Chapter 4 Problem 29
2. (5 pts) Chapter 4 Problem 30
3. (5 pts) Chapter 4 problem 31
4. (5 pts) Chapter 4 Problem 33
5. (5 pts) Chapter 4 Problem 35
6. (5 pts) Chapter 4 Problem 36
7. (5 pts) Chapter 4 Problem 41
8. (5 pts) Chapter 4 Problem 43
9. (5 pts) Chapter 4 Problem 44
10. (20 pts) MATLAB Problem

Sum of a Binomial Number of Independent Uniform Random Variables

Suppose you live in a small town of a hundred people and you own a small store. Every normal day (excluding Sundays of course) each person in the town has the probability  $p = 0.25$  of visiting your store. A person that visits your store will spend money distributed uniformly from 0 to 50 dollars. The amount of money spent in your store on any normal day is  $Y$ .

- a) Analytically compute the following: mean of  $Y$ , standard deviation of  $Y$  (consider page 242 in the book).
- b) Simulate this problem in the following fashion (turn in your code):  
Do the following loop 10,000 times
  - Generate the number of people,  $n$ , that visit your store every day by a Binomial random variable.
  - Sum together  $n$  random variables with uniform distributions from 0 to 50.
  - Store the sum of money - this is one outcome of the random variable  $Y$ .After the loop is complete, then compute the mean and standard deviation of the outcomes for  $Y$ .
- c) Plot a histogram representing the pdf of  $Y$ .
- d) Do the simulated values you computed in part b) match the values in part a)?