

## Dean's Lecture

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- 11 am tomorrow
- JSB Auditorium
- Counts for one of two lectures required in this class
- Be there early to get a seat!

1

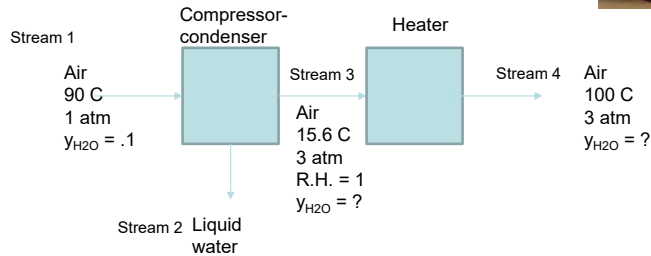
## Professional Program Application

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- Required in order to get an add code for ChEn 374 (Fluid Dynamics)
- We will discuss this **after Exam 2**
- You will need to see your faculty advisor
  - Course planning worksheet completed
  - Discuss grades in major courses
  - Ask for advice
- **Due November 18**

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# HW Review



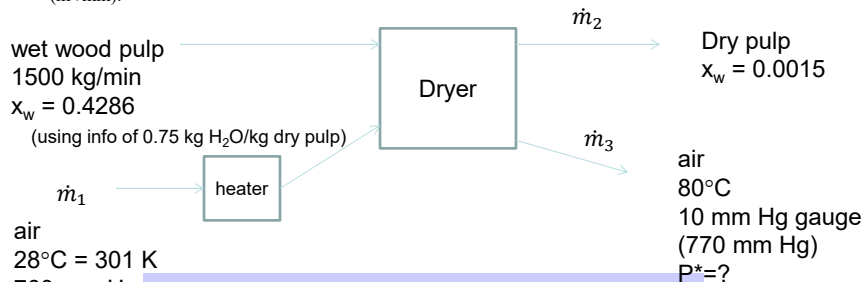
1. Use a basis of 100 moles of moist air entering compressor
2. Find  $y_{H_2O,3}$  from vapor pressure,  $RH_3$ , and definition of partial pressure
3. Note that  $y_{H_2O,3} = \frac{n_{H_2O,3}}{n_{H_2O,3} + n_{dry\ air}}$ , so if you know  $y_{H_2O,3}$  and  $n_{dry\ air}$ , you can get  $n_{H_2O,3}$
4. Do the balances on moles of water in and out of compressor
5. Use ideal gas law to get ratios of volumetric flow rates

Photo from <http://headinthesandblog.org/2016/11/parents-enough-hours-day-much-homework/>

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17.3. A hot-air dryer is used to reduce the moisture content of 1500 kg/min of wet wood pulp from 0.75 kg H<sub>2</sub>O/kg dry pulp to 0.15 wt% H<sub>2</sub>O. Air is drawn from the atmosphere at 28°C, 760 mm Hg, and 50% relative humidity, sent through a blower-heater, and then fed to the dryer. The air leaves the dryer at 80°C and 10 mm Hg (gauge). A sample of the exit air is drawn into a chamber containing a mirror and cooled slowly, keeping the gauge pressure at 10 mm Hg. A mist is observed to form on the mirror at a temperature of 40.0°C.

- (a) What is the vapor pressure of H<sub>2</sub>O at the conditions in the dryer exit?
- (b) Calculate the partial pressure and mole fraction of H<sub>2</sub>O in the air leaving the dryer.
- (c) Calculate the mass of water removed from the pulp (kg/min) and the volumetric flow rate of air entering the system (m<sup>3</sup>/min).



Strategy:

1.  $P^*_{out,3}$  at 40°C is dew point (from table) = F
2. Get  $y_{w,out,3}$  from  $P_{H_2O}/P_{tot}$  in the 40°C sample
3. Get  $y_{H_2O,in,1}$  from  $RH_{in}$
4. Balances on
  1. dry pulp mass
  2. moles of water
  3. moles of dry air

From cooled sample,  
 $P^* = 55.324$  mm Hg at 40 C, so  
 $y_{H_2O,3} = 55.324/770 = .07185$ ,  
 which is the same  $y_{H_2O,3}$  at  
 80C!  
 $RH = y_{H_2O}P_{tot}/P^*(80\ C) =$   
 $.07185 \cdot 770/355.1 = .156$ , or  
 15.6% RH in stream 3

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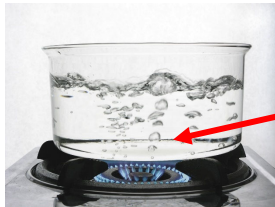
## Review



For a vessel with pure  $\text{H}_2\text{O}$  at 10 bar and  $100^\circ\text{C}$

- What is the vapor pressure?  $P_{\text{H}_2\text{O}}^* = 1 \text{ atm}$
- How much vapor is there?

0% vapor since it is pure  $\text{H}_2\text{O}$  and  $P_{\text{tot}} > P_{\text{H}_2\text{O}}^*$



What is the composition of the gas in the bubbles?

100% water vapor

How could you use Raoult's Law to find the temperature of the bubbles, given a total pressure?

Since  $P = P_{\text{H}_2\text{O}}^*$  at this interface (pure  $\text{H}_2\text{O}$ ), find  $T$  where  $P_{\text{H}_2\text{O}}^* = P_{\text{tot}}$

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## Review



One morning the weatherman said that the temperature was  $34^\circ\text{F}$  and the dew point was  $33^\circ\text{F}$ .

What does this mean?  $1^\circ\text{F}$  superheat

Relative Humidity was reported as 99%.

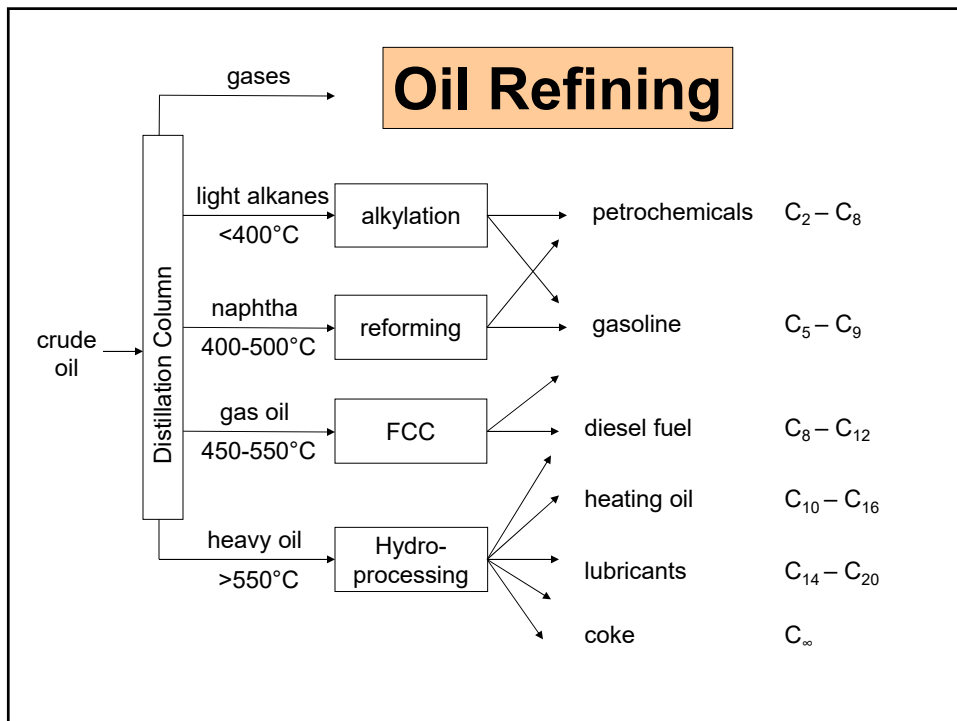
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## Class 19

### Multicomponent Vapor-Liquid Equilibrium

- Why Multicomponent?
- Review Raoult's Law
- Henry's Law
- Dew Point Calculation
- Bubble Point Calculation
- Flash Calculation

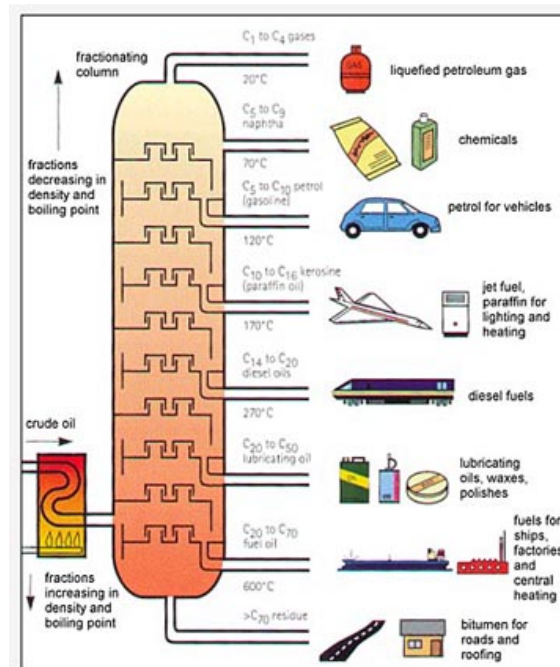
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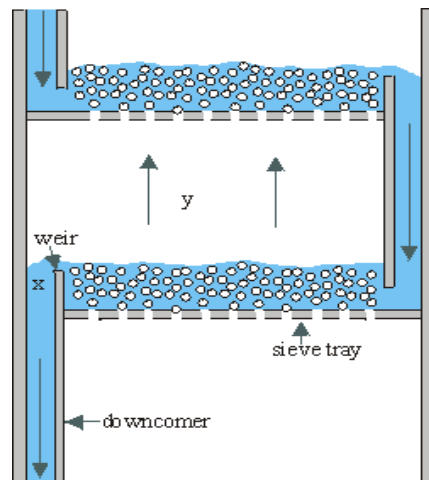


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# Distillation Column Trays

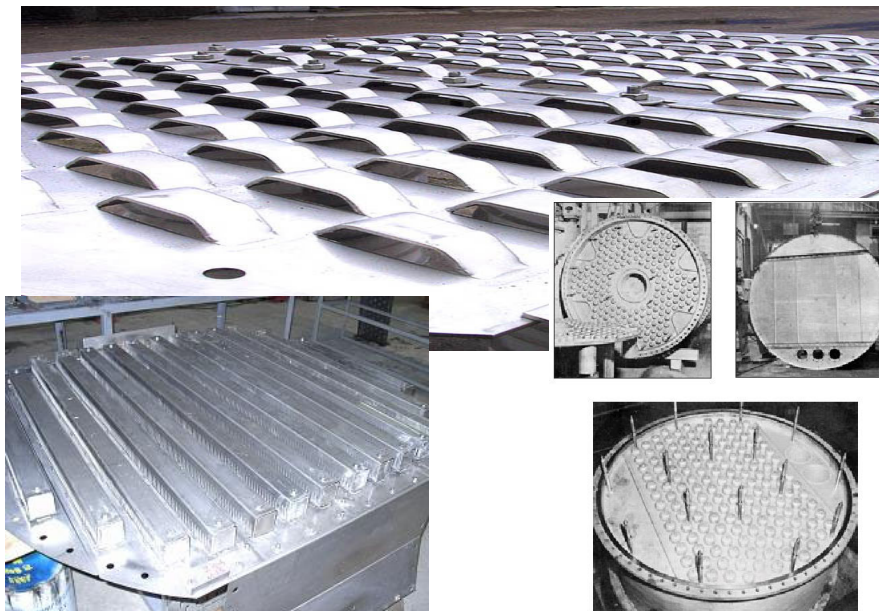


- On each tray, mixing is high enough to approach vapor-liquid equilibrium
- Vapor is enriched in more volatile component
- Liquid is enriched in less volatile component
- Multiple trays used to achieve greater separation yields

<https://www.youtube.com/watch?v=bzAjbwiasfE>

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## Trays in Distillation Column



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# Henry's Law

(in place of Raoult's Law)

- Raoult's Law when  $x_i \rightarrow 1$ 
  - $P_i = x_i P_i^*$
- Henry's Law used when  $x_i \rightarrow 0$ 
  - $P_i = x_i H_i$
  - $H_i$  is Henry's Law constant
  - $H_i = f(T)$
  - Tables available, but not in our book

Table 1: Some forms of Henry's law and constants (gases in water at 298 K), derived from [4]

equation:	$k_{H,pc} = \frac{p}{c}$	$k_{H,cp} = \frac{c}{p}$	$k_{H,px} = \frac{p}{x}$	$k_{H,cc} = \frac{c_{aq}}{c_{gas}}$
units:	$\frac{L \cdot atm}{mol}$	$\frac{mol}{L \cdot atm}$	atm	dimensionless
O <sub>2</sub>	769.23	$1.3 \times 10^{-3}$	$4.259 \times 10^4$	$3.180 \times 10^{-2}$
H <sub>2</sub>	1282.05	$7.8 \times 10^{-4}$	$7.099 \times 10^4$	$1.907 \times 10^{-2}$
CO <sub>2</sub>	29.41	$3.4 \times 10^{-2}$	$0.163 \times 10^4$	0.8317
N <sub>2</sub>	1639.34	$6.1 \times 10^{-4}$	$9.077 \times 10^4$	$1.492 \times 10^{-2}$
He	2702.7	$3.7 \times 10^{-4}$	$14.97 \times 10^4$	$9.051 \times 10^{-3}$
Ne	2222.22	$4.5 \times 10^{-4}$	$12.30 \times 10^4$	$1.101 \times 10^{-2}$
Ar	714.28	$1.4 \times 10^{-3}$	$3.955 \times 10^4$	$3.425 \times 10^{-2}$
CO	1052.63	$9.5 \times 10^{-4}$	$5.828 \times 10^4$	$2.324 \times 10^{-2}$

where:

$c$  = amount concentration of gas in solution (in mol/L)  
 $p$  = partial pressure of gas above the solution (in atm)  
 $x$  = mole fraction of gas in solution (dimensionless)

(from Wikipedia)

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# Henry's Law

(in place of Raoult's Law)

Find the equilibrium mole fraction of O<sub>2</sub> in water if air above water is at 298 K

- $k_{H,px,O_2} = 4.259e4 \text{ atm}$
- $P_{O_2} = x_{O_2} k_{H,px,O_2}$
- But  $P_{O_2} = 0.21 \text{ atm}$
- $x_{O_2} = P_{O_2}/k_{H,px,O_2}$
- So  $x_{O_2} = .21 \text{ atm}/4.259e4 \text{ atm}$

Mole fraction of O<sub>2</sub> in water = 4.9e-6, or 4.6 parts per million (ppm)

Table 1: Some forms of Henry's law and constants (gases in water at 298 K), derived from [4]

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where:

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(from Wikipedia)

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## Terms you should know

- **VLE**
  - Vapor-liquid equilibrium
- **Bubble point calculation**
  - Any VLE calculation where  $x_i$  is known
  - T or P known, find  $y_i$  and P or T
- **Dew point calculation**
  - Any VLE calculation where  $y_i$  is known
  - T or P known, find  $x_i$  and P or T
- **Flash calculation**
  - VLE calculation where feed composition ( $z_i$ ) is known along with T and  $P_{\text{tot}}$  of output
  - Need to find  $x_i$ 's,  $y_i$ 's, and L and V

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## Think....

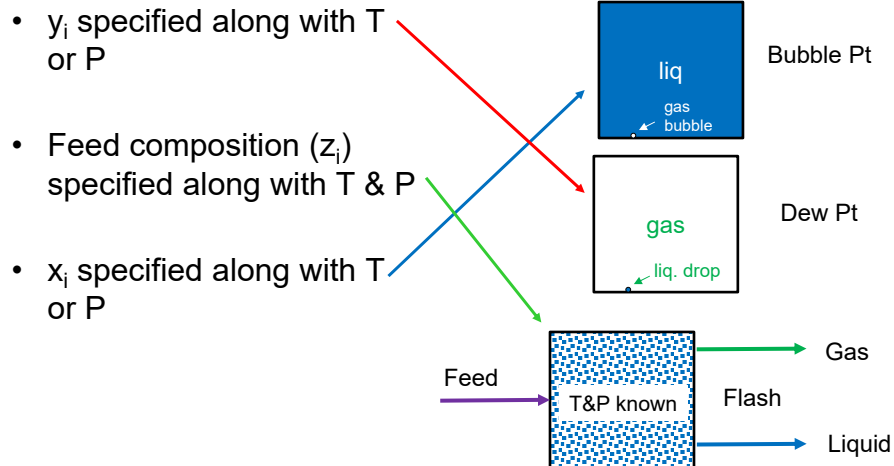
- A closed vessel has a mixture of 50% benzene and 50% toluene
  - $T_{b, \text{benzene}} = 80.1^\circ\text{C}$
  - $T_{b, \text{toluene}} = 110.62^\circ\text{C}$       These  $T_b$ 's are at 1 atm
- Suppose you have this mixture at 1 atm and  $25^\circ\text{C}$ 
  - What phases are present?      All liquid since  $T < T_{\text{boil}}$  for both species
  - If you start heating the mixture, at what T will you start to get gas (assuming P stays constant)?       $80.1^\circ\text{C}$
  - What will be the composition of the initial gas?      100% benzene
  - How will the gas composition change as you continue to heat the mixture?      More and more toluene will vaporize
  - If the mixture is heated to  $111^\circ\text{C}$ , what will be the composition of the gas phase?      50% benzene and 50% toluene, just like initial liquid composition
  - What if you had a blanket of  $\text{N}_2$  above the liquid?
    - $\text{N}_2$  could "suck up" benzene and toluene at T's below the boiling point based on  $P^*$ 's

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# Matching

(2 + species, VLE)

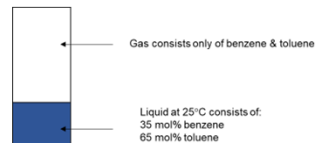


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# Handouts

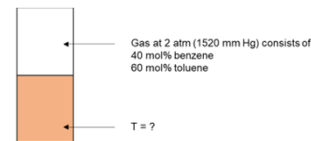
- Bubble pt calculation

Find:  $P_{\text{sat}}$ ,  $y_i$ ,  $y_T$

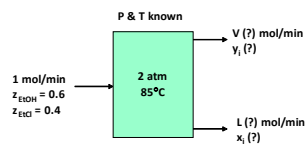


- Dew pt calculation

Find:  $T$ ,  $x_i$ ,  $x_T$



- Flash calculation



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## Summary of Multicomponent Vapor-Liquid Equilibrium (VLE)

- $x_i$  known (bubble point calculation)

- If  $P_{\text{tot}}$  given, guess  $T$  to satisfy  $P_{\text{tot}} = \sum P_i = \sum x_i P_i^*$
- If  $T$  given, get  $P_{\text{tot}} = \sum x_i P_i^*$
- Then  $y_i = x_i P_i^* / P_{\text{tot}}$

Note: this only works  
If there is no non-condensable  
gas above the liquid.

- $y_i$  known (dew point calculation)

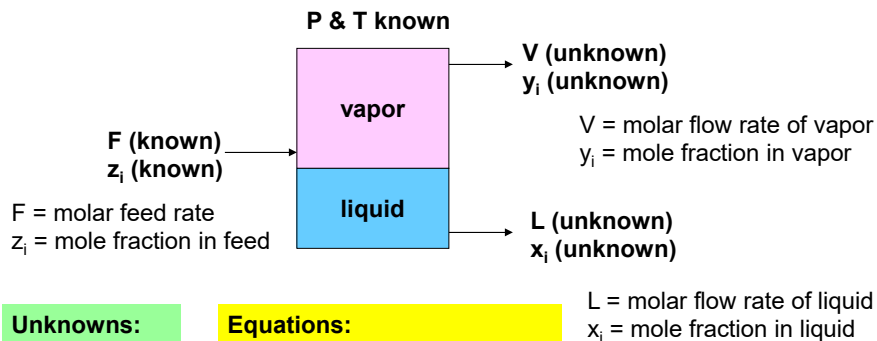
- Use relation:  $\sum x_i = 1$
- If  $P_{\text{tot}}$  given, guess  $T$  to satisfy  $\sum \frac{y_i P_{\text{tot}}}{P_i^*} = 1$
- If  $T$  given, get  $P_{\text{tot}} = \frac{1}{\sum \frac{y_i}{P_i^*}}$
- Then  $y_i = x_i P_i^* / P_{\text{tot}}$

Write in book!

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## Flash Calculation



**Unknowns:**

$V, L$	2
$y_i$ 's	$n-1$
$x_i$ 's	$n-1$
<b>Total</b>	<b>2n</b>

**Equations:**

$x_i P_i^* = y_i P_{\text{tot}}$	$n$
<u>Species balances</u>	<u><math>n</math></u>
<b>Total</b>	<b>2n</b>

(Only  $n-1$   $x_i$ 's because  $\sum x_i = 1$ )

Alternate:  $P$  known and  $y_i$  known

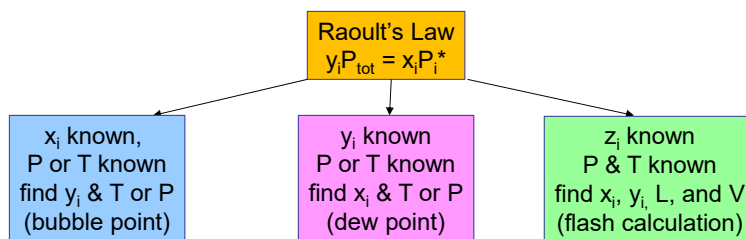
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# Flash Calculation

- $z_i$ 's known, 2 species, P&T known
  - Raoult's law for each species
    - $y_1 P_{\text{tot}} = x_1 P_1^*$
    - $(1-y_1) P_{\text{tot}} = (1-x_1) P_2^*$
    - Add these equations to get:  $P_{\text{tot}} = x_1 P_1^* + (1-x_1) P_2^*$
    - Solve for  $x_1$
    - Get  $y_1 = x_1 P_1^* / P_{\text{tot}}$
  - Mole balances
    - $F = V + L$
    - $z_1 F = y_1 V + x_1 L$
    - 2 equations, 2 unknowns (V & L)
- $z_i$ 's known, multiple species → Solver

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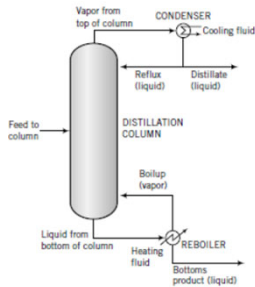
## Multicomponent Logic Chart



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## Hint on Prob 18.1

(b) Find T of vapor leaving top of column



Note that there is a tray near the top of the column that has liquid in equilibrium with the vapor leaving the column. This becomes a dew point problem since you know the vapor composition. The unknown is the temperature, which determines the vapor pressure of each species (just like the problem we did in class --- see next slide).

(c) Find T of reboiler

Since you calculated the composition of the bottoms product stream, which is a liquid, this is a bubble point problem to find the temperature (similar to part b except for a bubble point)

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	A	B	C	D	E	F	G	H	I
1	<b>Dew Point Example to find temperature</b>								
2	<b>Given</b>								
3	y_benz=	0.4							
4	y_tol=	0.6							
5	Ptot=	2 atm							
6		1520 mm Hg							
7	T	127.0 C	<==== Guess						
8		400.0 K							
9	<b>Antoine Equation</b>								
10	P*_benz=	2648.8 mm Hg	6.89272	1203.531	219.888			Temp Range ( C)	
11	P*_tol=	1183.7 mm Hg	6.95805	1346.773	219.693				
12	Function = 1 - sum(y_i * Ptot/P*_i)								
13	Function=	5.95452E-07							
14	Beyond T range of P* correlations???								
15									
16	<b>xi Pi* = yi Ptot</b>								
17	x_benz=	0.230							
18	x_tol=	0.770							
19	Sum=	1.0							
20									

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# Extra Notes

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## Bubble Point, or if $x_i$ 's known

- $x_i$ 's known,  $y_i$ 's wanted (n unknowns)
- P or T given, T or P wanted (1 unknown)

**Total unknowns: n+1**

### Equations

- $x_i P_i^* = y_i P_{\text{tot}}$  (n eqns)
- $\sum y_i = 1$  (1 eqn)

- Strategy: Solve for  $y_i$ , then sum all equations to eliminate the unknown  $y_i$  because  $\sum y_i = 1$

$$y_i = x_i P_i^* / P_{\text{tot}}$$

Summing both sides,

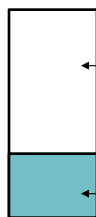
$$\sum y_i = 1 = \sum (x_i P_i^* / P_{\text{tot}})$$

- If T known, calculate  $P_i^*$ 's, solve for  $P_{\text{tot}}$ , then use Raoult's law to get  $y_i$ 's
- If  $P_{\text{tot}}$  known, guess T, find  $P_i^*$ 's, see if  $\sum (x_i P_i^* / P_{\text{tot}}) = 1$   
 - ITERATE

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## "Bubble Point" Example

Find:  $P_{\text{tot}}$ ,  $y_B$ ,  $y_T$



Gas consists only of benzene & toluene

Liquid at 25°C consists of:  
40 mol% benzene  
60 mol% toluene

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## Dew Point, or if $y_i$ 's known

- $y_i$ 's known,  $x_i$ 's wanted (n unknowns)
- P or T given, T or P wanted (1 unknown)

**Total unknowns: n+1**

### Equations

- $x_i P_i^* = y_i P_{\text{tot}}$  (n eqns)
- $\sum x_i = 1$  (1 eqn)

- Strategy: Solve for  $x_i$ , then sum all equations to eliminate the unknown  $x_i$  because  $\sum x_i = 1$

$$x_i = (y_i \cdot P_{\text{tot}} / P_i^*)$$

Summing both sides,

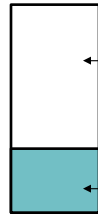
$$\sum x_i = 1 = P_{\text{tot}} \sum (y_i / P_i^*)$$

- If T known, solve for  $P_{\text{tot}}$ , then use Raoult's law to get  $x_i$ 's
- If  $P_{\text{tot}}$  known, guess T, find  $P_i^*$ 's, see if  $P_{\text{tot}} \sum (y_i / P_i^*) = 1$   
- ITERATE

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## "Dew Point" Example

Find:  $T$ ,  $x_B$ ,  $x_T$



Gas at 2 atm (1520 mm Hg) consists of  
40 mol% benzene  
60 mol% toluene

Liquid consists of:  
? mol% benzene  
? mol% toluene

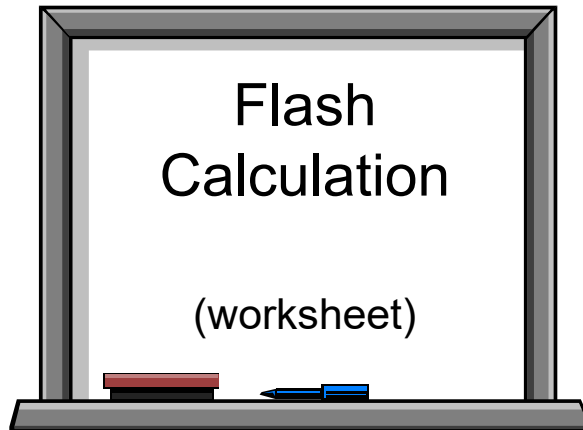
Why is this a dew  
point example when  
there is quite a bit of  
liquid?



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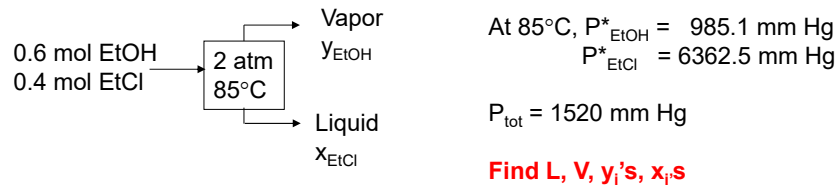
## Flash Calculation

(worksheet)



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## Sample Flash Calculation



Mole Balance:  $1 = V + L$   
EtOH Balance:  $0.6 = y_{\text{EtOH}}V + x_{\text{EtOH}}L$

Raoult's Law:  $\frac{y_{\text{EtOH}}P}{(1-y_{\text{EtOH}})P} = \frac{x_{\text{EtOH}}P^*_{\text{EtOH}}}{(1-x_{\text{EtOH}})P^*_{\text{EtCl}}}$  Add these two equations

$$P = x_{\text{EtOH}}P^*_{\text{EtOH}} + (1-x_{\text{EtOH}})P^*_{\text{EtCl}}$$

Solve for x  $x_{\text{EtOH}} = \frac{P - P^*_{\text{EtCl}}}{P^*_{\text{EtOH}} - P^*_{\text{EtCl}}} = \frac{1520 - 6362.5}{985.1 - 6362.5} = 0.9$  so  $x_{\text{EtCl}} = 0.1$

Using Raoult's law:  $y_{\text{EtOH}}(1520) = (0.9)(985.1)$  so  $y_{\text{EtOH}} = 0.583$   
 $y_{\text{EtCl}} = 0.417$

Now use mole balances:  $1 = V + L$   
 $0.6 = 0.583V + 0.9L$  2 eqns, 2 unknowns:  $L = 0.0536$   
 $V = 0.9464$

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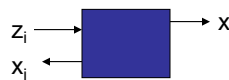
## Hint on 18.2 (replaced in 2021)

### A. Partial condenser



- However, at minimum pressure,  $m_{\text{liq}} \rightarrow 0$ , so  $y_i$  is known ( $= z_i$ )
- If  $y_i$  is known, this is a dew point calculation!
  - T known, find P!

### B. Total condenser



- However, at minimum pressure,  $m_{\text{vap}} \rightarrow 0$ , so  $x_i$  is known ( $= z_i$ )
- If  $x_i$  is known, this is a bubble point calculation!
  - T known, find P!

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