Chemical Engineering 374

Fluid Mechanics

Pipe Networks



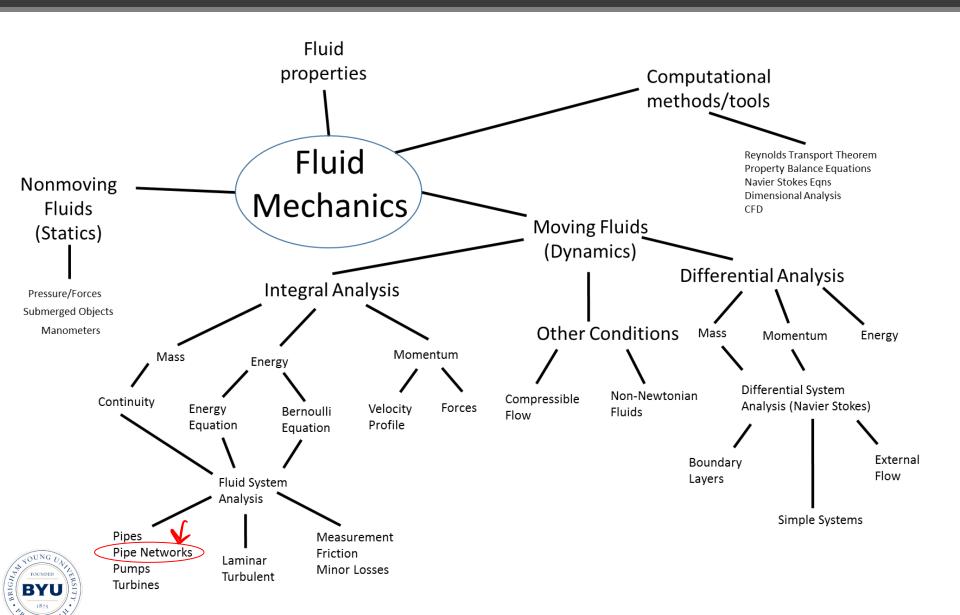
Spiritual Thought

Alma 26:22

22 Yea, he that repenteth and exerciseth faith, and bringeth forth good works, and prayeth continually without ceasing—unto such it is given to know the mysteries of God; yea, unto such it shall be given to reveal things which never have been revealed; yea, and it shall be given unto such to bring thousands of souls to repentance, even as it has been given unto us to bring these our brethren to repentance.



Fluids Roadmap



Key Points

- Pipe Networks composed of single pipes
- Pipes is series
 - Type I find ΔP
 - Type II find \dot{V}
 - Type III or IV find D, Find L Doesn't work!!
- Pipes in parallel
 - Type I
 - Type II
 - Type III or IV Find D, Find L Doesn't work



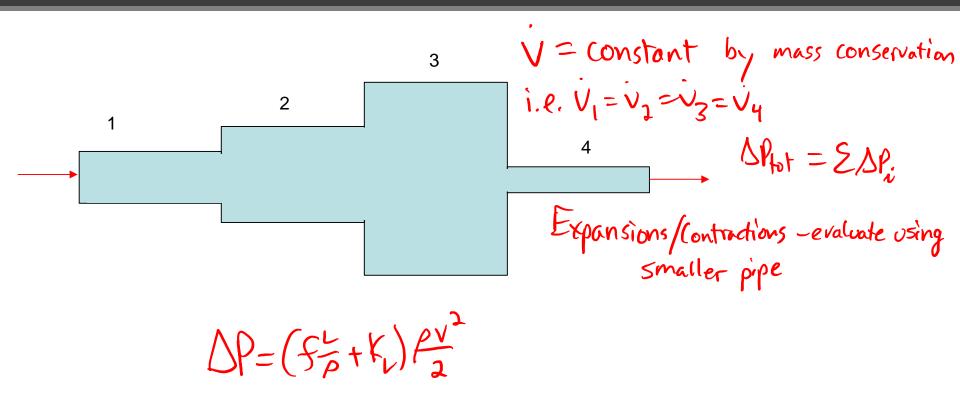
KNOW graphical solution method!!!!

Pipe Networks

- Most systems are not single pipes
 - Central heating in home
 - Nuclear reactor cooling systems
 - Water supply for cities
 - Oil/product pipes in refineries
 - Etc.
- Can be decomposed into series/parallel
- Similar analysis to electrical circuits



Pipes in Series (I)

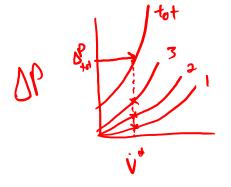


• Type 1 problem: Know L, D, \dot{V} , then find ΔP

Pipes in Series (II)

Type 2 problem: Know ΔP, D, L, then find V

- system demand curve > SP for any possible v



or som AP up to find total system curve read off i from SP tot vs V conve

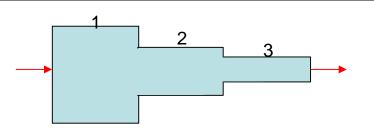
· Or solve
$$\Delta P_t = \sum_{i}^{L_i} \frac{\rho v_i^2}{2} f_i$$
 using colbrook for f_i

-> solve the nonlinear equations



Type III or II -> not unique, cont solve!

Series Example



	L (m)	D (m)	ε (m)
1	100	0.05	0.00024
2	150	0.045	0.00012
3	80	0.04	0.0002

 $\Delta P_t = 320,000 \text{ Pa}$; ignore K_L

 $S_i = S_i(Re_i, \epsilon_i)$

Re = PVilli

Find v?

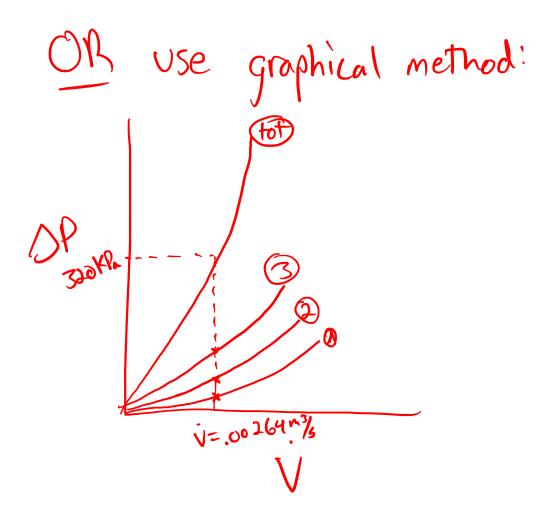
$$\Delta P_1 + \Delta P_2 + \Delta P_3 = \Delta P_t$$

$$\Delta P_1 = f_1 \frac{L_1}{D_1} \frac{V^2 P_2}{V^2}$$

$$\Delta P_2 = f_3 \frac{L_1}{D_1} \frac{V^2 P_2}{V^2}$$

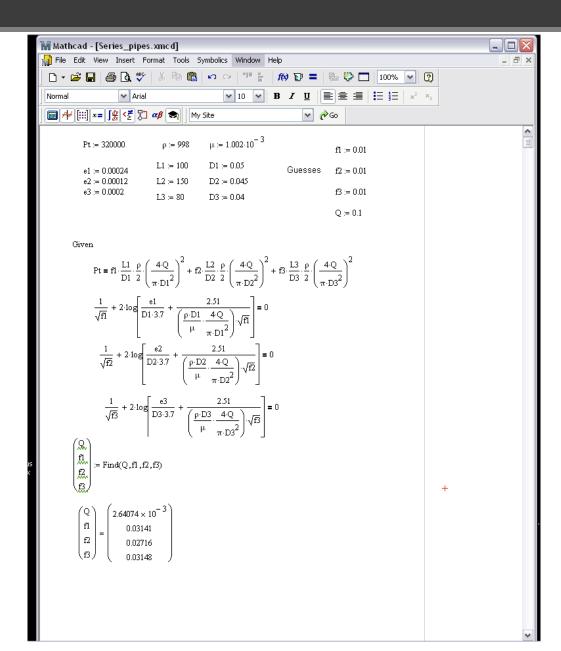


Graphical Series



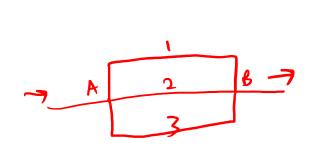


MathCAD solution (Pipes in Series)





Pipes in Parallel (I)



$$\dot{V}_{\text{tot}} = \dot{V}_1 + \dot{V}_2 + \dot{V}_3$$

 $V_{tot} = V_1 + V_2 + V_3$ $\frac{2}{3} = \frac{3}{3}$ $\frac{3}{3} = \frac{3}{3$ any poth)

Type I: V, Known, SP& Vtot Unknown: Find SP - calculate SP, using V,, Then W/SP Calculate V2, V3 (type II problem) $\dot{V}_1 + \dot{V}_2 + \dot{V}_3 = \dot{V}_{tot}$



Pipes in Parallel (II)

Type II: AP known, flow rates unknown

(alculate type II problem for each pipe

Vtot = V, +V2 + V3

System demand curve

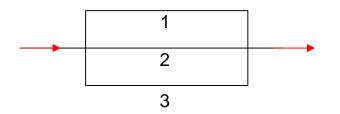


Pipes in Parallel (III)

- Type I: Total flow rate (Vtot) known OP unknown - System demand corve: sum to the right: or solve multiple eq. numerically via Python or Math (AD

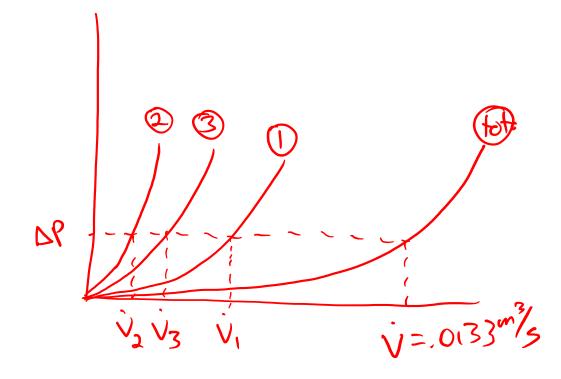


Parallel Example



	L (m)	D (m)	ε (m)
1	100	0.05	0.00024
2	150	0.045	0.00012
3	80	0.04	0.0002

 \dot{V} = .0133 m³/s Pa; Find Δ P





MathCAD solution (Parallel Pipes)

