

Chemical Engineering 378

Science of Materials Engineering

Lecture 15

Failure and Fractures



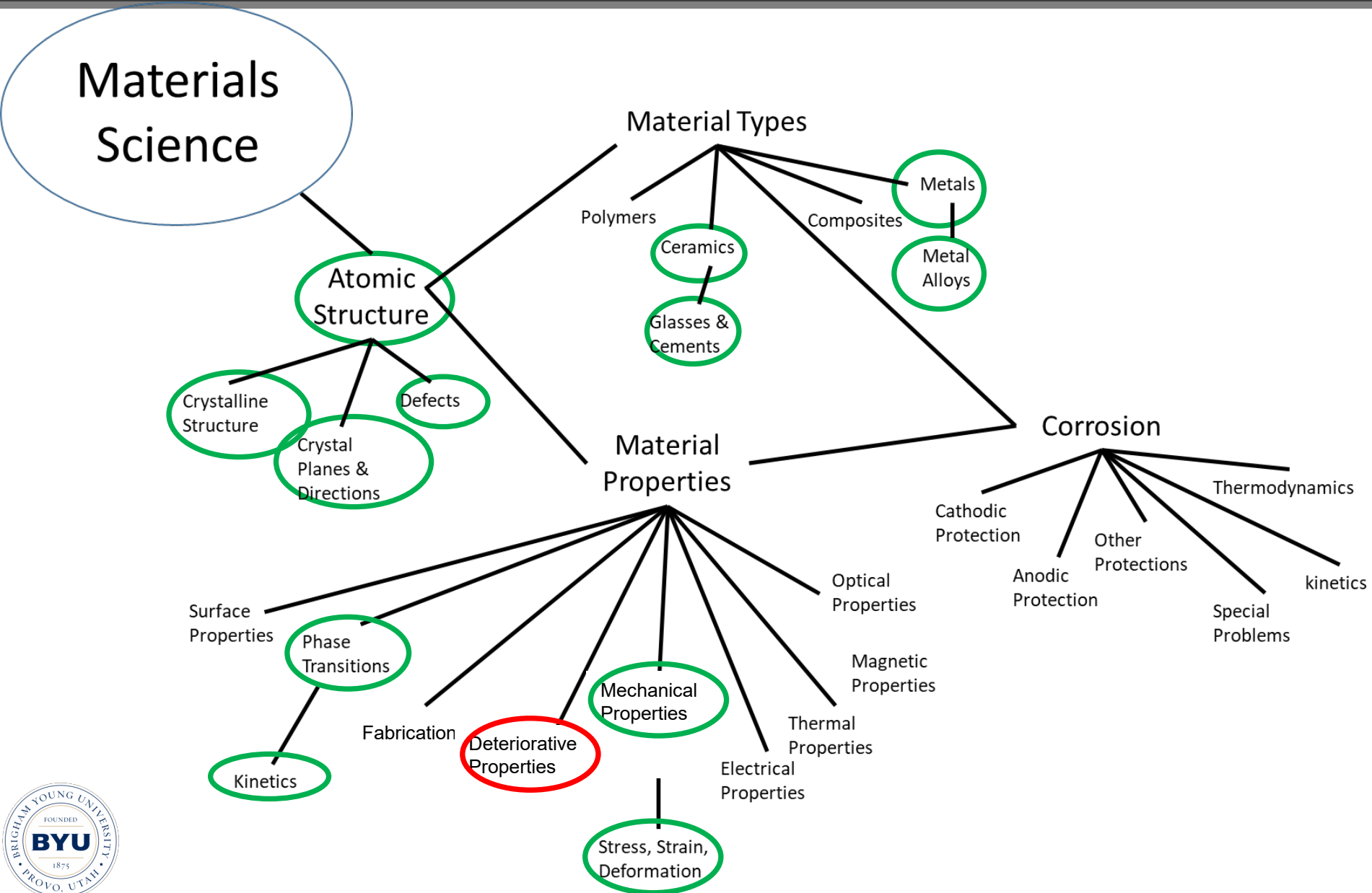
Spiritual Thought

Moroni 7:48

48. Wherefore, my beloved brethren, pray unto the Father with all the energy of heart, that ye may be filled with this love, which he hath bestowed upon all who are **true followers of his Son, Jesus Christ; that ye may become the sons of God...**

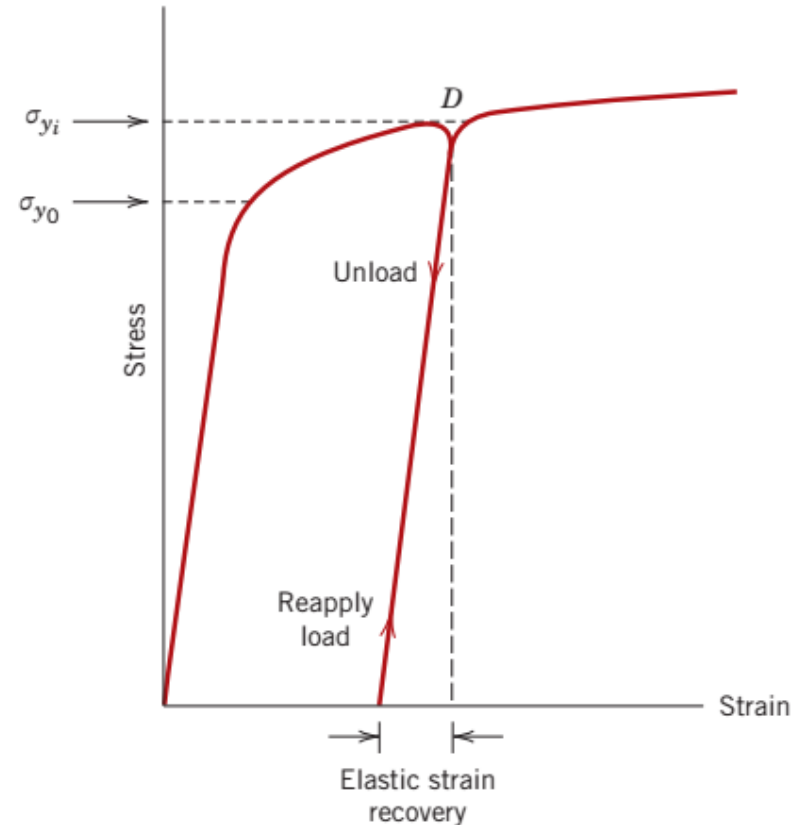
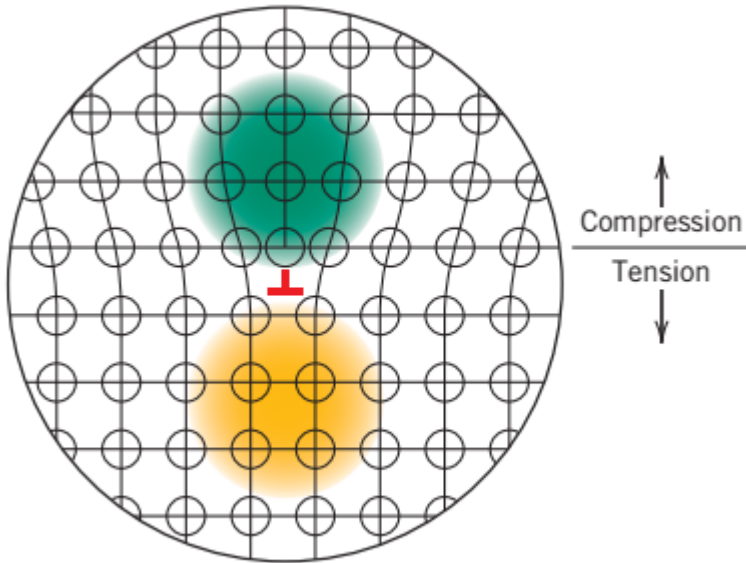


Materials Roadmap



Strain Hardening

- Strain Hardening: The process by which ductile metal becomes harder as it is plastically deformed.



Strain Hardening

Figure 7.5 (a) Two edge dislocations of the same sign and lying on the same slip plane exert a repulsive force on each other; C and T denote compression and tensile regions, respectively. (b) Edge dislocations of opposite sign and lying on the same slip plane exert an attractive force on each other. Upon meeting, they annihilate each other and leave a region of perfect crystal.

(Adapted from H. W. Hayden, W. G. Moffatt, and J. Wulff, *The Structure and Properties of Materials*, Vol. III, *Mechanical Behavior*, John Wiley & Sons, 1965. Reproduced with permission of Kathy Hayden.)

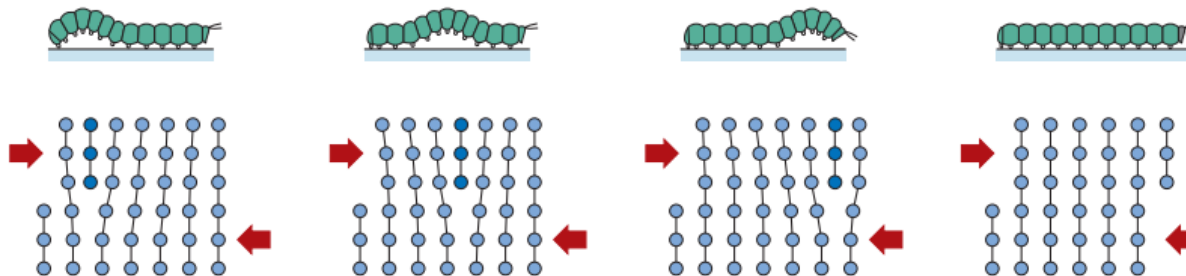
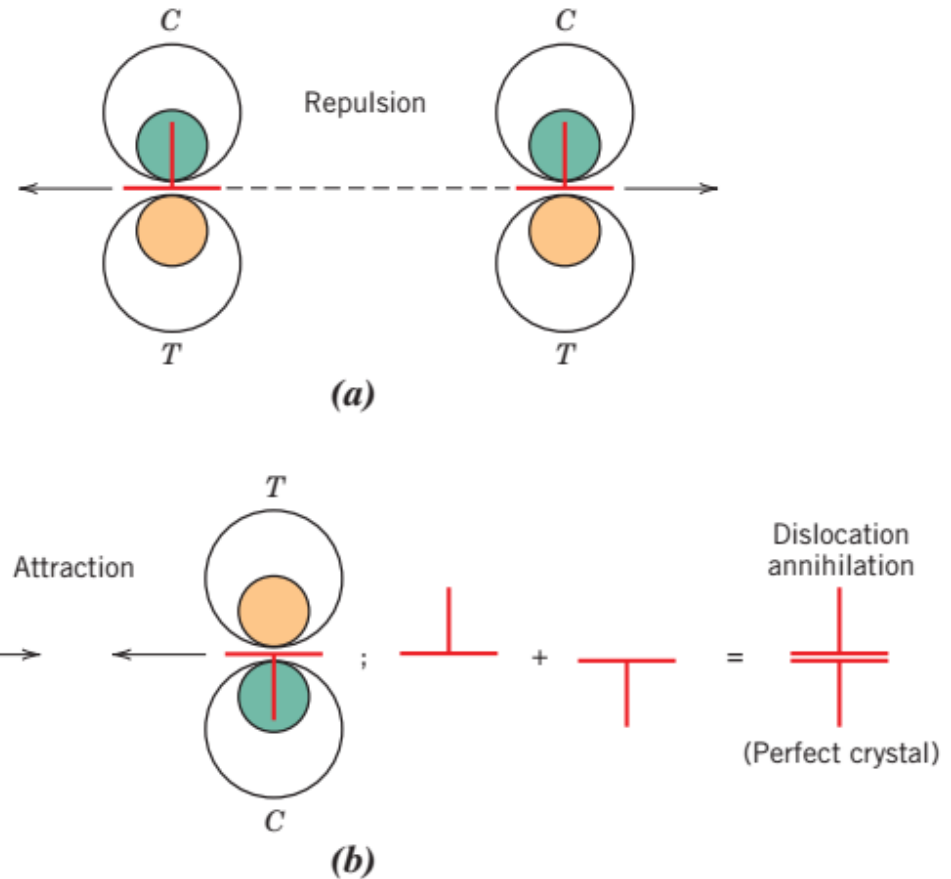


Figure 7.3 The analogy between caterpillar and dislocation motion.

Strain Hardening (cont.)

Dislocation Density and Cold Working

$$\text{Dislocation density} = \frac{\text{total dislocation length}}{\text{unit volume}}$$

- Dislocation density in undeformed metal
 - $10^5\text{-}10^6 \text{ mm}^{-2}$
- Dislocation density increases with increasing deformation
- Dislocation density in deformed (cold-worked) metal
 - $10^9\text{-}10^{10} \text{ mm}^{-2}$

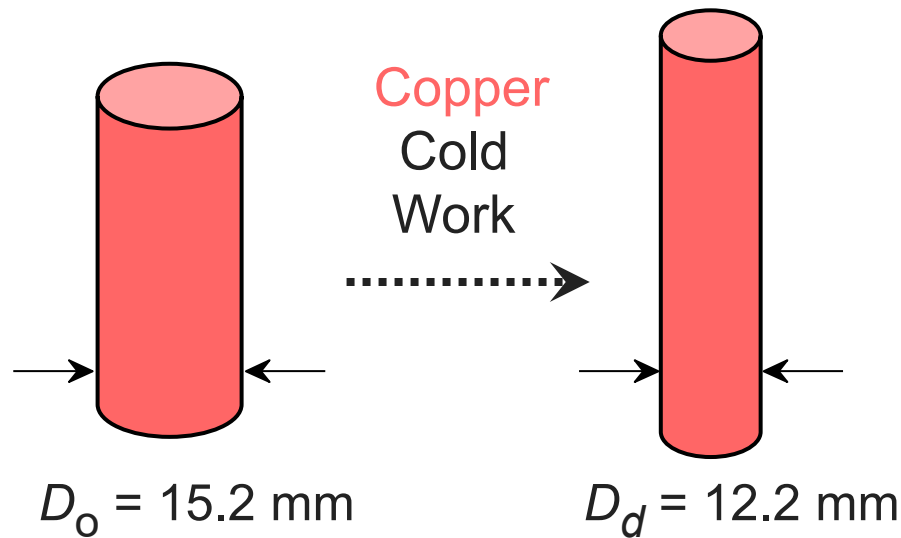


Affect of Cold Work on Mechanical Properties

7

Example Problem:

Compute the yield and tensile strengths, and ductility for a cylindrical Cu specimen that has been cold worked by reducing its diameter from 15.2 mm to 12.2 mm.



% cold worked

$$\%CW = \left(\frac{A_0 - A_d}{A_0} \right) \times 100$$

Example Problem (cont.)

- Solution:

$$\%CW = \frac{\cancel{\pi} \left(\frac{D_o}{\cancel{2}} \right)^2 - \cancel{\pi} \left(\frac{D_d}{\cancel{2}} \right)^2}{\cancel{\pi} \left(\frac{D_o}{\cancel{2}} \right)^2} \times 100$$

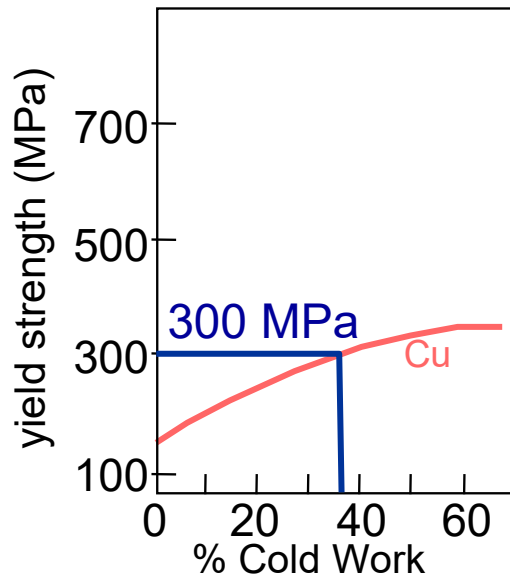
$$= \frac{D_o^2 - D_d^2}{D_o^2} \times 100$$

$$\%CW = \frac{(15.2 \text{ mm})^2 - (12.2 \text{ mm})^2}{(15.2 \text{ mm})^2} \times 100 = 35.6\%$$

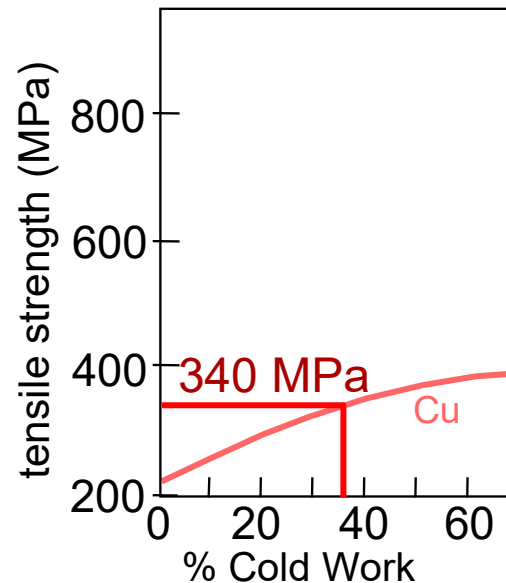


Example Problem (cont.)

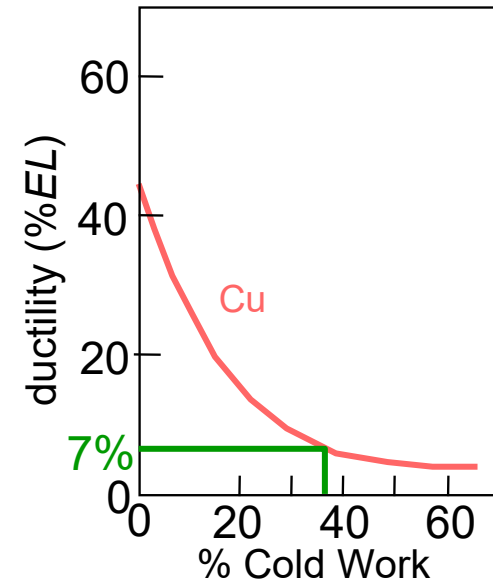
- Yield and tensile strength, and ductility (%EL) are determined graphically as shown below for %CW = 35.6%



$$\sigma_y = 300 \text{ MPa}$$



$$TS = 340 \text{ MPa}$$

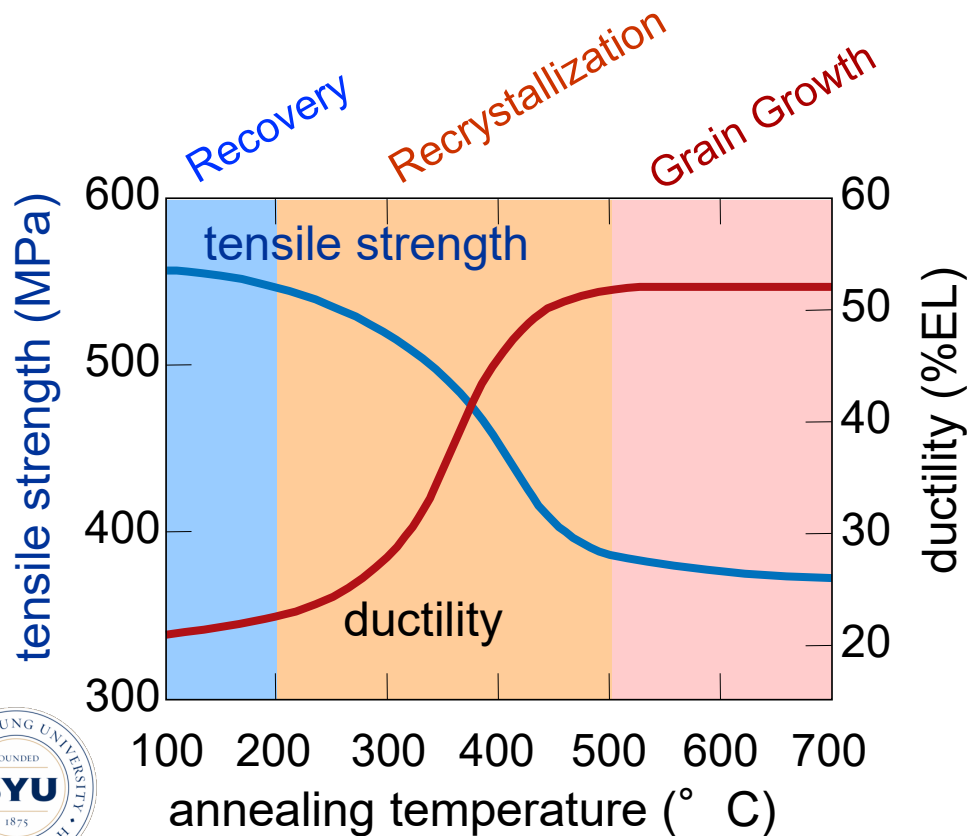


$$\%EL = 7\%$$

Fig. 7.19, Callister & Rethwisch 10e. [Adapted from *Metals Handbook: Properties and Selection: Irons and Steels*, Vol. 1, 9th edition, B. Bardes (Editor), 1978; and *Metals Handbook: Properties and Selection: Nonferrous Alloys and Pure Metals*, Vol. 2, 9th edition, H. Baker (Managing Editor), 1979. Reproduced by permission of ASM International, Materials Park, OH.]

Heat Treatment of Cold-Worked Metal Alloys

- **Heat treating** cold worked metals brings about changes in structure and properties
- As a result, effects of cold work are nullified!
- This type of heat treatment sometimes termed “**annealing**”
- 1 hour treatment at T_{anneal} decreases tensile strength & increases %EL



Three Annealing stages:

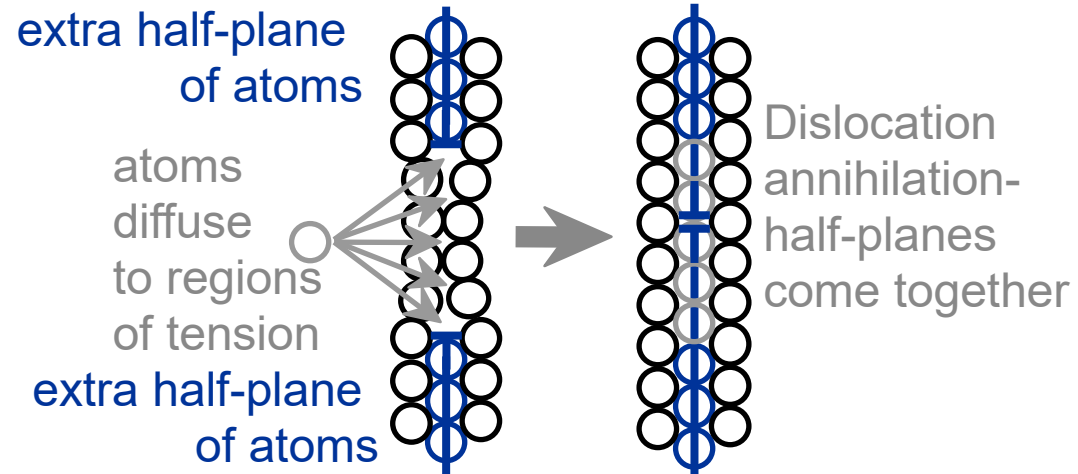
1. **Recovery** (100-200° C)
2. **Recrystallization** (200-500° C)
3. **Grain Growth** (> 500° C)

Fig. 7.22, *Callister & Rethwisch 10e*.
(Adapted from G. Sachs and K. R. Van Horn, *Practical Metallurgy, Applied Metallurgy and the Industrial Processing of Ferrous and Nonferrous Metals and Alloys*, 1940. Reproduced by permission of ASM International, Materials Park, OH.)

Recovery

During recovery – reduction in disl. density – annihilation of disl.

- Scenario 1

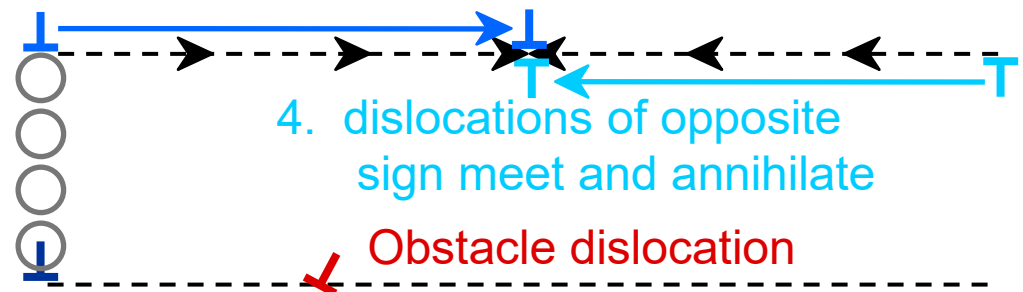


- Scenario 2

3. “Climbed” disl. can now move on new slip plane

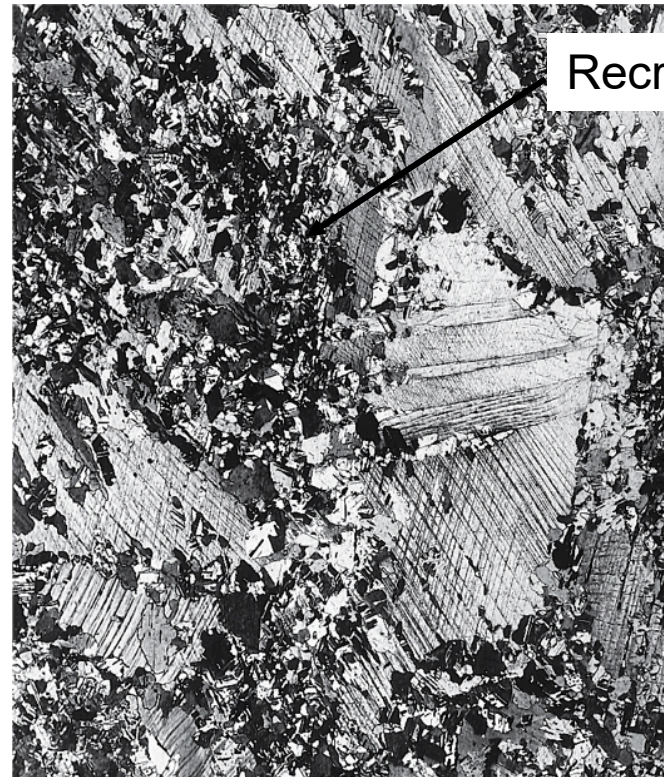
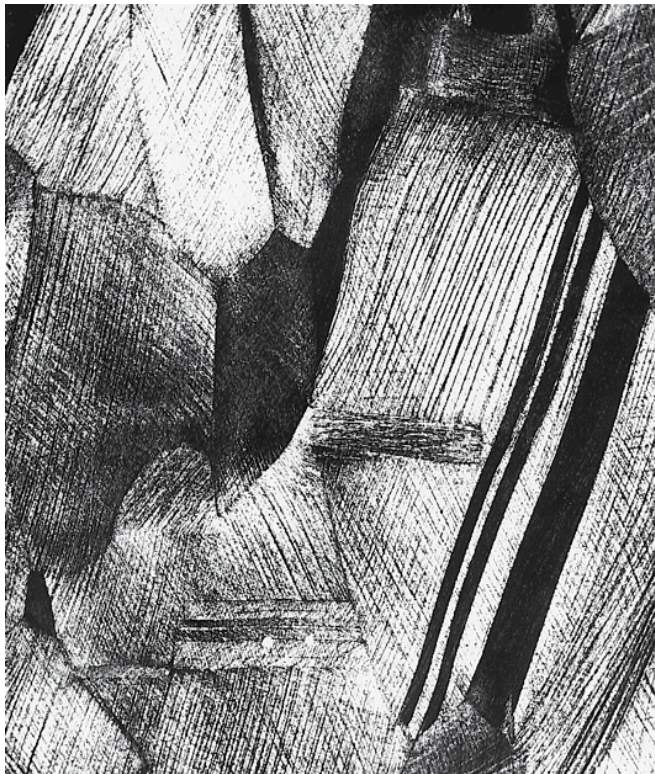
2. grey atoms leave by vacancy diffusion allowing disl. to “climb”

1. dislocation blocked; can’t move to the right



Recrystallization

- New grains form that:
 - have low dislocation densities
 - are small in size
 - consume and replace parent cold-worked grains.

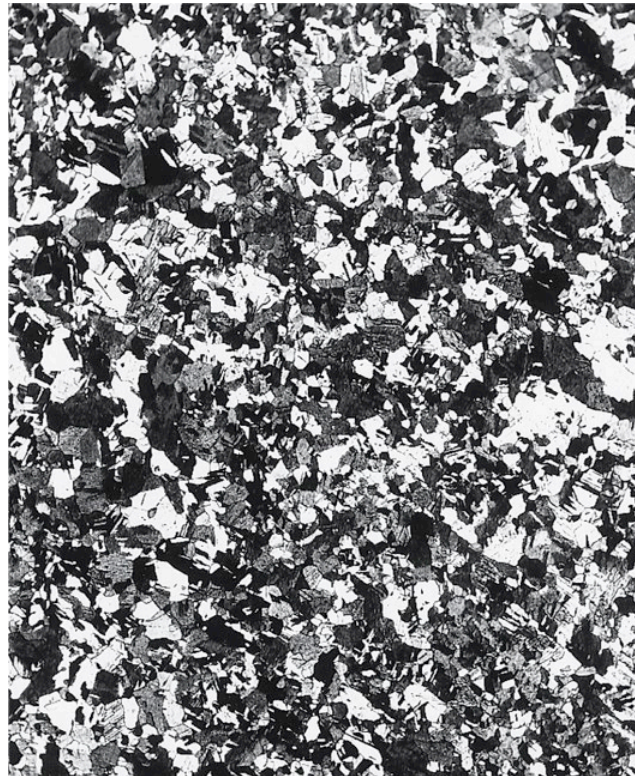


Recrystallized grains

Adapted from Fig. 7.21 (a),(c),
Callister & Rethwisch 10e.
(Photomicrographs courtesy of J.E. Burke, General Electric Company.)

Recrystallization (cont.)

- All grains in cold-worked material have been consumed/replaced.



After 8 sec. at 580° C

Adapted from Fig. 7.21 (d), *Callister & Rethwisch 10e*.
(Photomicrographs courtesy of J.E. Burke, General Electric Company.)

Recrystallization Temperature

T_R = recrystallization temperature = temperature at which recrystallization just reaches completion in 1 h.

$$0.3T_m < T_R < 0.6T_m$$

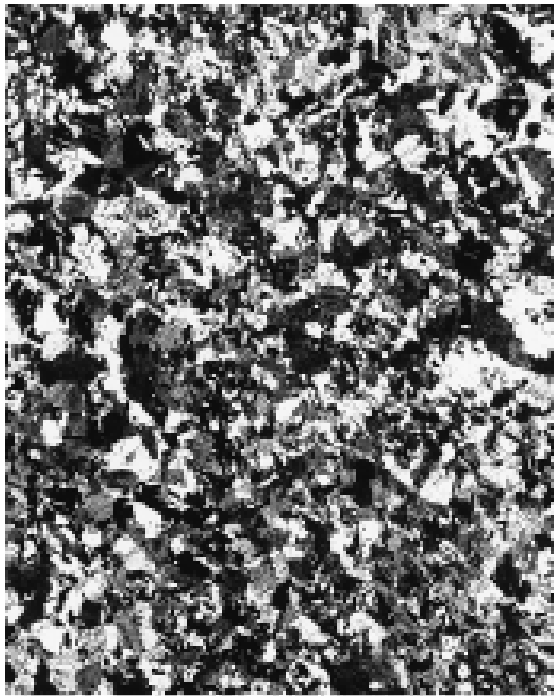
For a specific metal/alloy, T_R depends on:

- %CW -- T_R decreases with increasing %CW
- Purity of metal -- T_R decreases with increasing purity

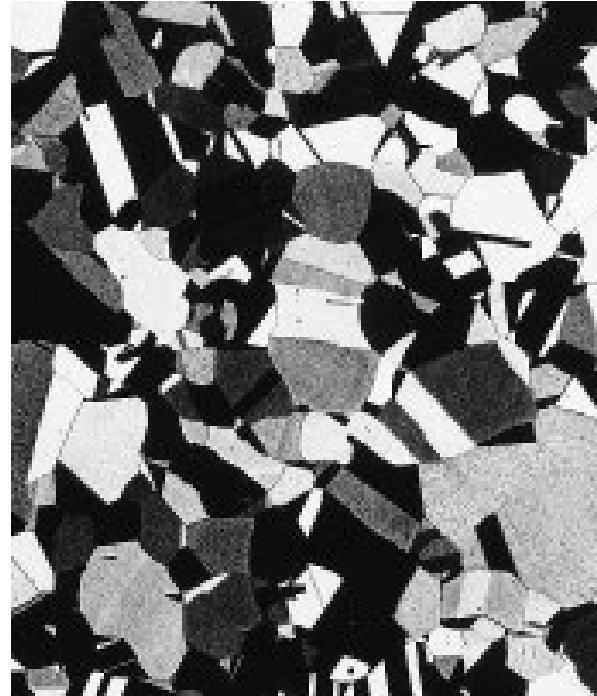


Grain Growth

- Grain growth occurs as heat treatment continues.
 - Average grain size increases
 - Small grains shrink (and ultimately disappear)
 - Large grains continue to grow



After 8 sec. at 580° C



After 15 min. at
580° C

Adapted from Fig.
9.21 (d),(e), *Callister
& Rethwisch 10e*.
(Photomicrographs
courtesy of J.E. Burke,
General Electric
Company.)

Grain Growth (cont.)

- Empirical relationship—dependence of average grain size (d) on heat treating time (t):

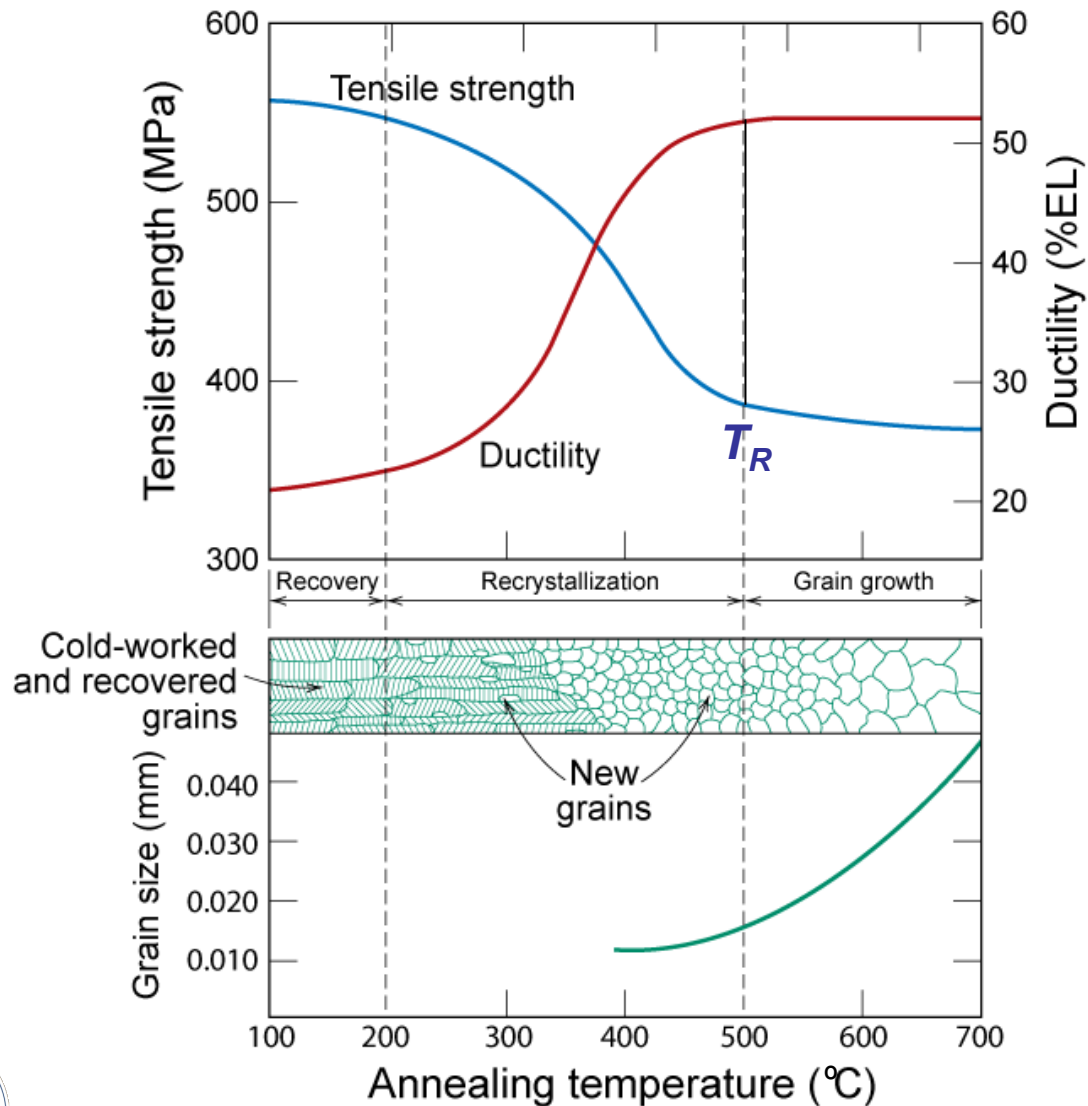
exponent typ. ~ 2

$$d^n - d_o^n = Kt$$

material constant
—depends on T
—independent of t

Initial average grain diam. before heat treatment

Recovery, Recrystallization, & Grain Growth

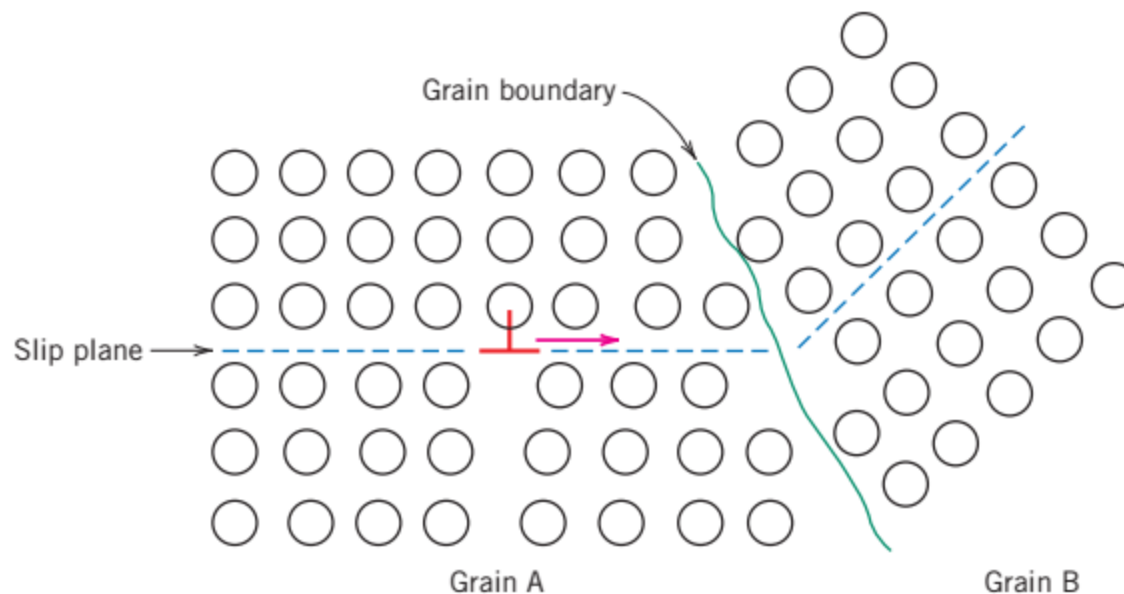


T_R = recrystallization temperature

annealing time = 1 h

Fig. 7.22, *Callister & Rethwisch 10e*.
(Adapted from G. Sachs and K. R. Van Horn, *Practical Metallurgy, Applied Metallurgy and the Industrial Processing of Ferrous and Nonferrous Metals and Alloys*, 1940. Reproduced by permission of ASM International, Materials Park, OH.)

Grain Size Effects Strength



Yield Strength

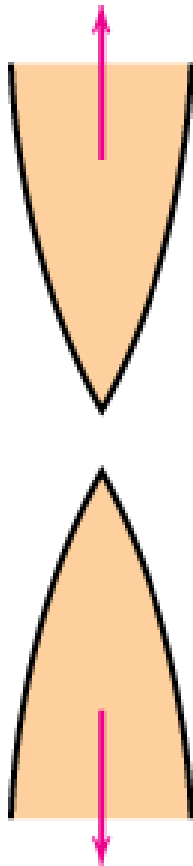
$$\sigma_y = \sigma_0 + k_y d^{-1/2}$$

Average Grain Diameter

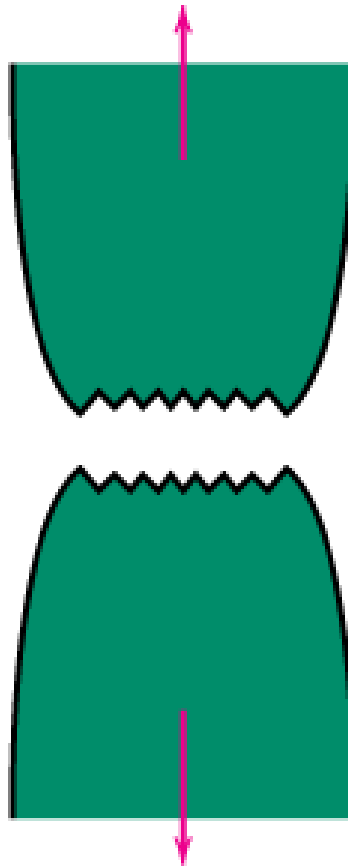
Material Property Constants

Fracture Profiles

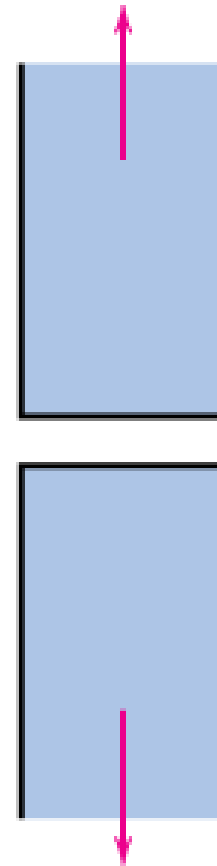
Very
Ductile



Moderately
Ductile



Brittle



Adapted from Fig. 8.1, *Callister & Rethwisch 10e*.

Fracture Surface Photographs



cup-and-cone fracture
- moderately ductile

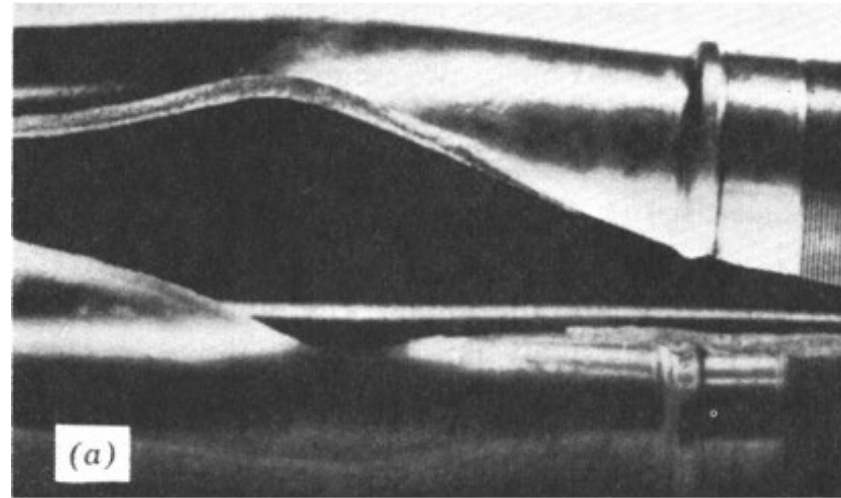


brittle fracture
- totally brittle
- flat surfaces

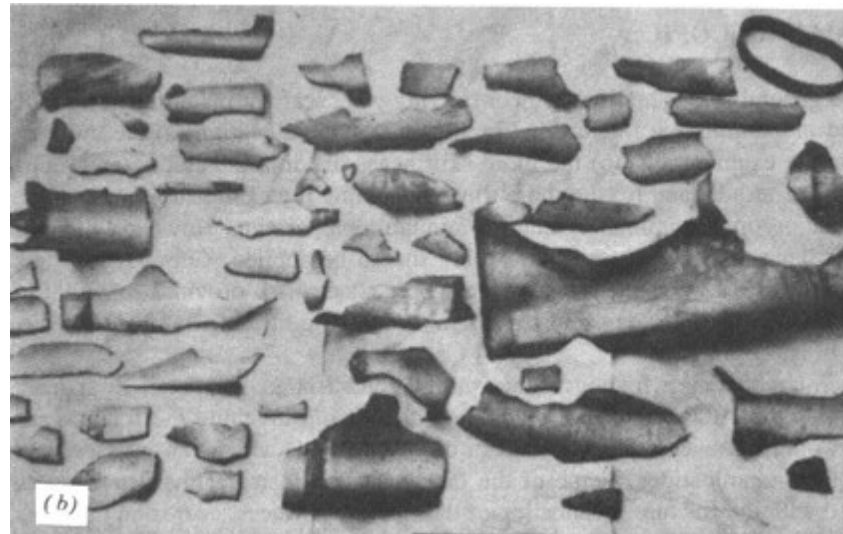
Fig. 8.3, *Callister & Rethwisch 10e.*

Examples of Ductile and Brittle Fracture of Pipes

- **Ductile fracture:**
 - one piece
 - large deformation

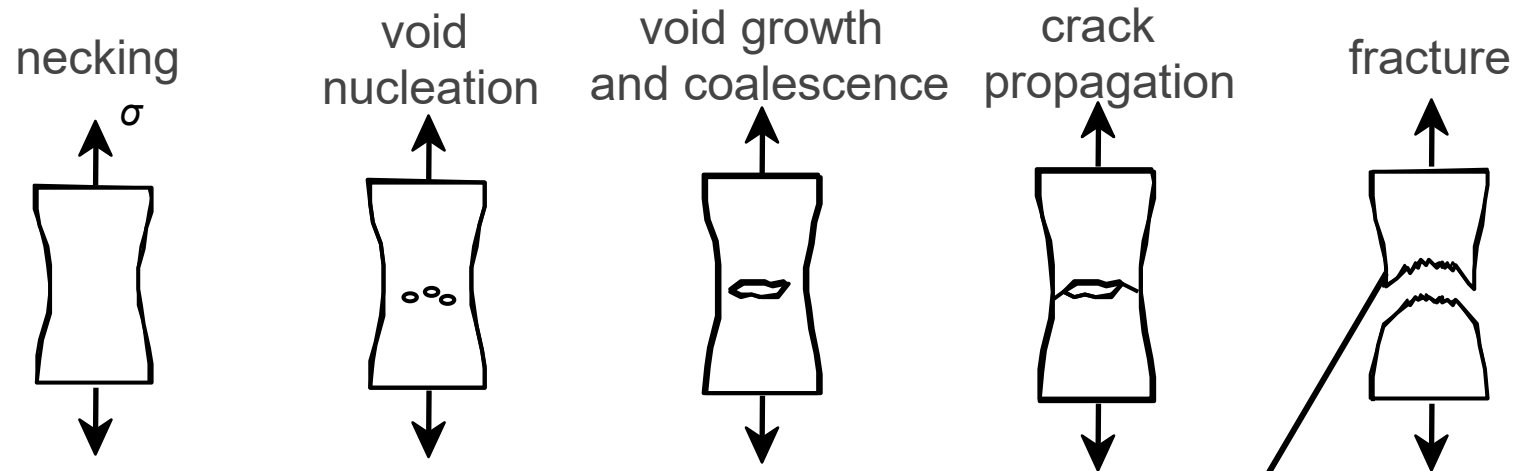


- **Brittle fracture:**
 - many pieces
 - small deformations



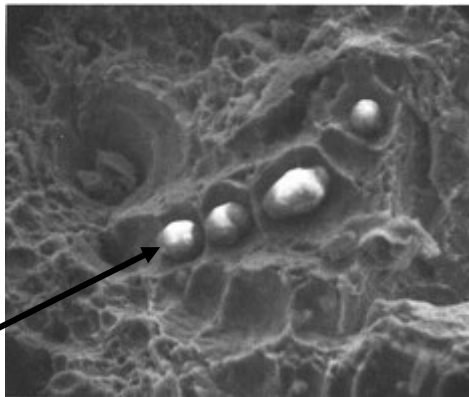
Figures from V.J. Colangelo and F.A. Heiser, *Analysis of Metallurgical Failures* (2nd ed.), Fig. 4.1(a) and (b), p. 66 John Wiley and Sons, Inc., 1987. Used with permission.

Stages of Moderately Ductile Failure

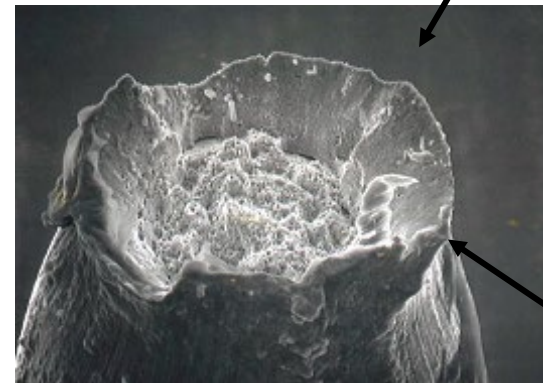


- Electron micrographs of fracture surfaces (steel)

particles serve as void nucleation sites.



From V.J. Colangelo and F.A. Heiser, *Analysis of Metallurgical Failures* (2nd ed.), Fig. 11.28, p. 294, John Wiley and Sons, Inc., 1987. (Orig. source: P. Thornton, *J. Mater. Sci.*, Vol. 6, 1971, pp. 347-56.)



Fracture surface of tire cord wire loaded in tension. Courtesy of F. Roehrig, CC Technologies, Dublin, OH. Used with permission.

cup and cone fracture surface

Brittle Failure Surface Photographs

- Brittle fracture surface displays V-shaped, chevron markings
- V features point to the crack initiation site

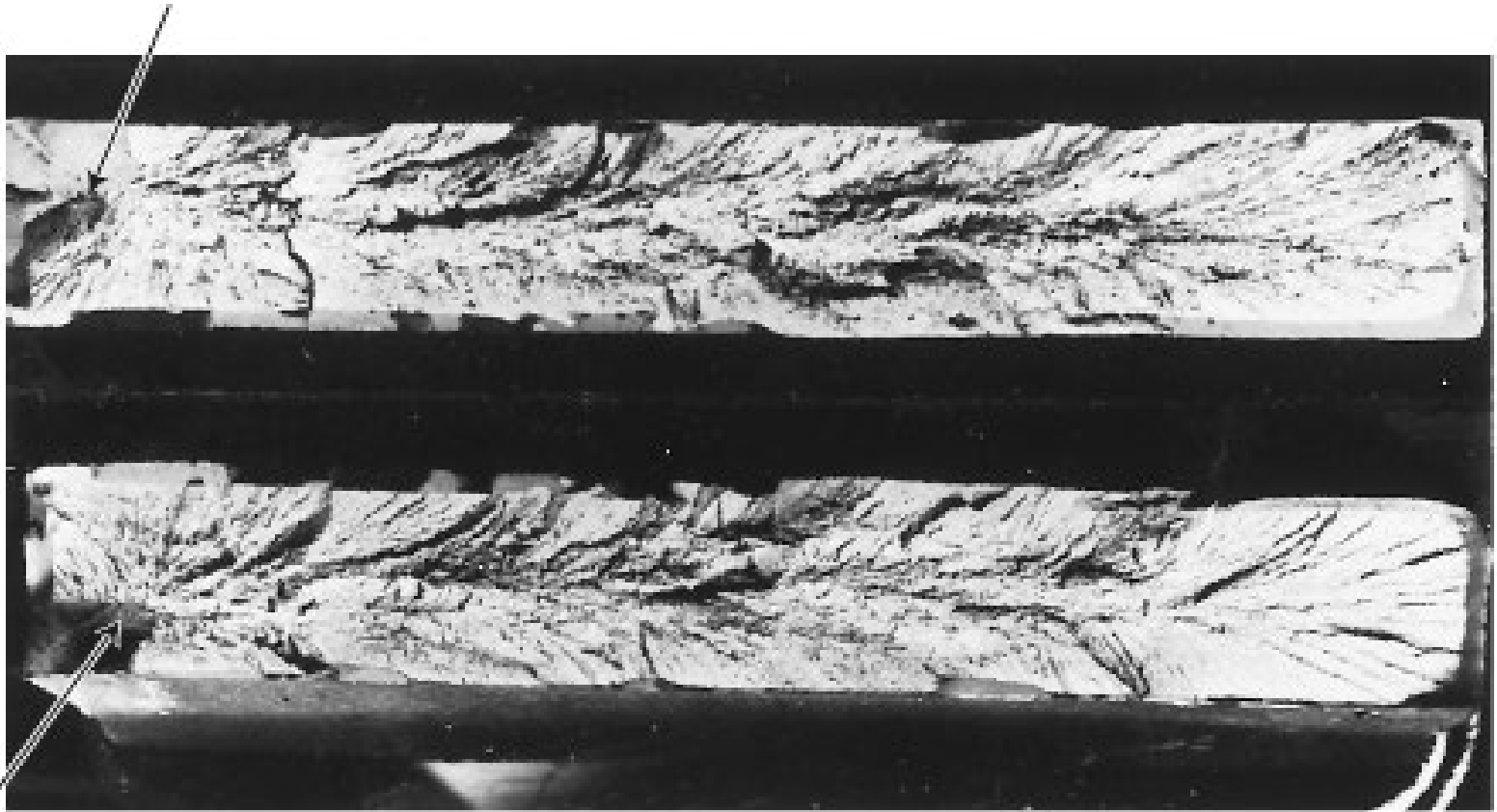
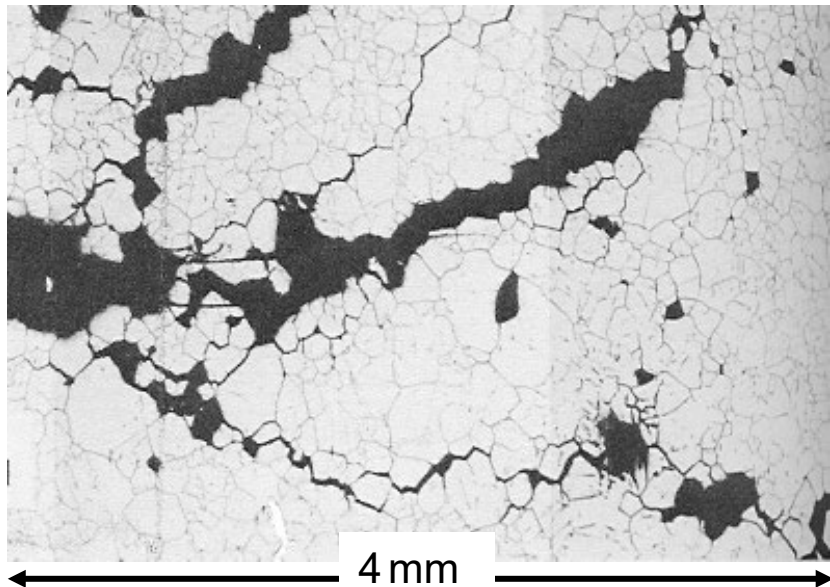


Fig. 8.5(a), *Callister & Rethwisch 10e*. [From R. W. Hertzberg, *Deformation and Fracture Mechanics of Engineering Materials*, 3rd edition. Copyright © 1989 by John Wiley & Sons, New York. Reprinted by permission of John Wiley & Sons, Inc. Photograph courtesy of Roger Slutter, Lehigh University.]

Photographs of Brittle Fracture Surfaces

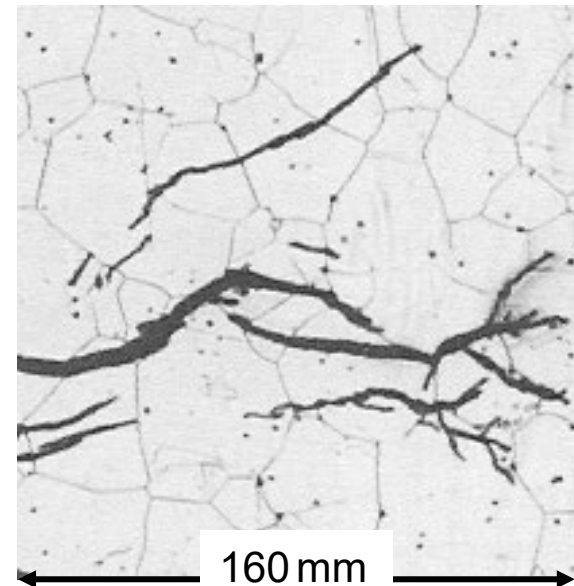
- **Inter**granular crack propagation (**between** grains)



304 S. Steel (metal)

Reprinted w/permission from "Metals Handbook", 9th ed, Fig. 633, p. 650. Copyright 1985, ASM International, Materials Park, OH. (Micrograph by J.R. Keiser and A.R. Olsen, Oak Ridge National Lab.)

- **Trans**granular crack propagation (**through** grains)



316 S. Steel (metal)

Reprinted w/ permission from "Metals Handbook", 9th ed, Fig. 650, p. 357. Copyright 1985, ASM International, Materials Park, OH. (Micrograph by D.R. Diercks, Argonne National Lab.)

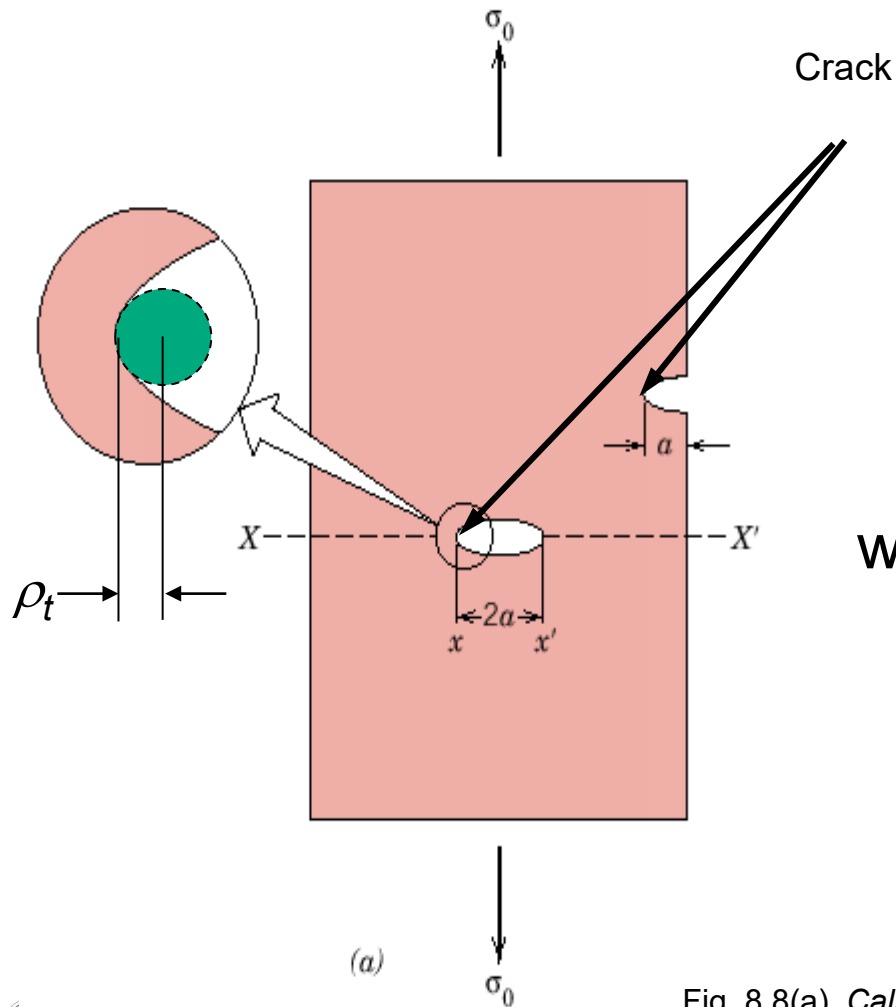
Principles of Fracture Mechanics

- Fracture occurs as result of crack propagation
- Measured fracture strengths of most materials much lower than predicted by theory
 - microscopic flaws (cracks) always exist in materials
 - magnitude of applied tensile stress amplified at the tips of these cracks



Fracture Mechanics (cont.)

Flaws are Stress Concentrators!



$$\sigma_m = 2\sigma_o \left(\frac{a}{\rho_t} \right)^{1/2}$$

where

ρ_t = radius of curvature

σ_o = applied stress

σ_m = stress at crack tip

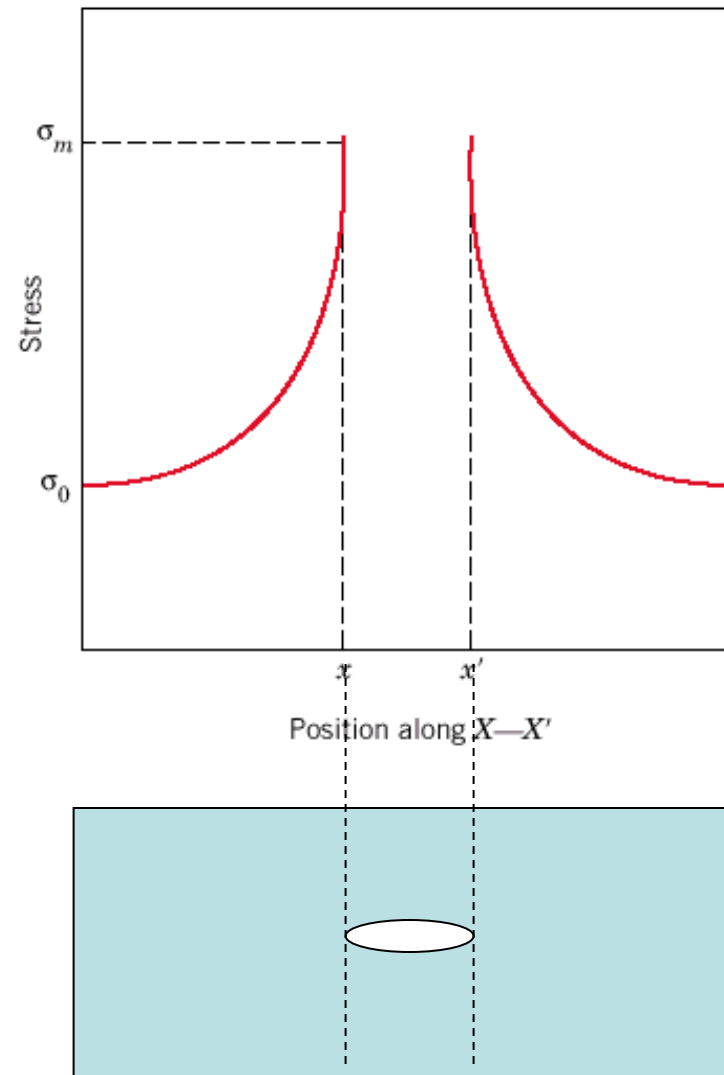
Fig. 8.8(a), Callister & Rethwisch 10e.

Fracture Mechanics (cont.)

Stress Concentration at Crack Tip

K_t = stress concentration factor

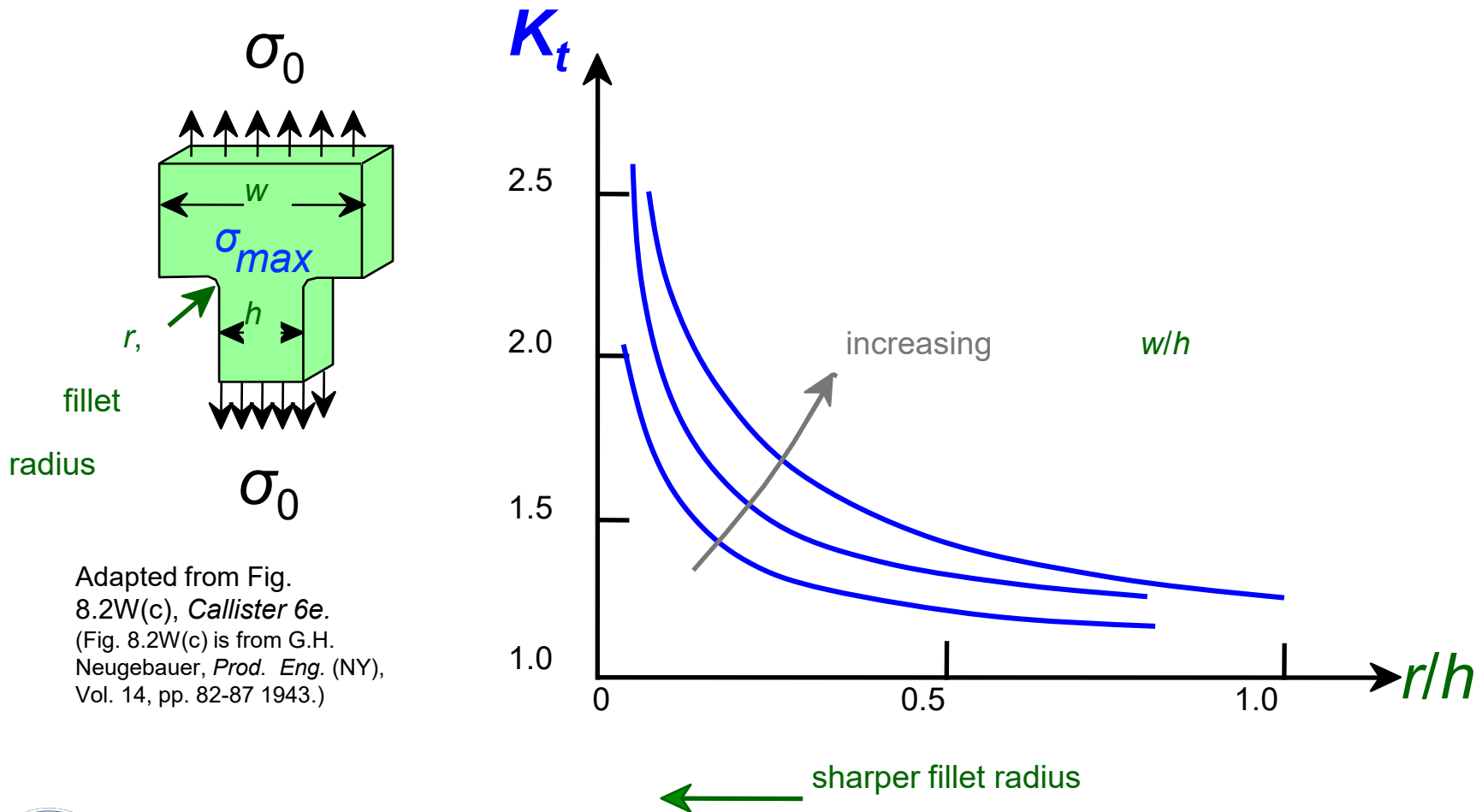
$$K_t = \frac{\sigma_m}{\sigma_o}$$



Adapted from Fig. 8.8(b),
Callister & Rethwisch 10e.

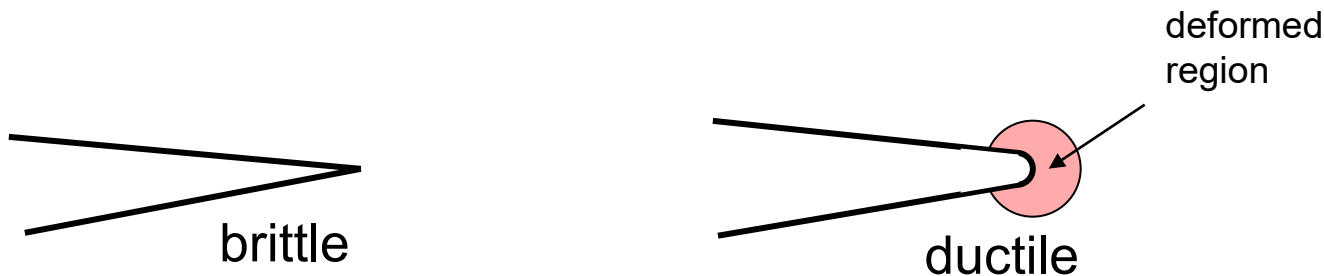
Fracture Mechanics (cont.)

- **Avoid sharp corners!**



Crack Propagation

- Stress concentration higher for sharp cracks—propagate at lower stresses than cracks with blunt tips
- For ductile materials—plastic deformation at crack tip when stress reaches yield strength—tip blunted—lowers stress conc.



Criterion for Crack Propagation

Critical stress for crack propagation (σ_c) of brittle materials

$$\sigma_c = \left(\frac{2E\gamma_s}{\pi a} \right)^{1/2}$$

where

- σ_c = crack-tip stress
- E = modulus of elasticity
- γ_s = specific surface energy
- a = one half length of internal crack

For ductile materials
replace γ_s with $\gamma_s + \gamma_p$
where γ_p is plastic
deformation energy

- materials have numerous cracks with different lengths and orientations
- crack propagation (and fracture) occurs when $\sigma_m > \sigma_c$ for crack with lowest σ_c

- Largest, most highly stressed cracks grow first!

