

# Chemical Engineering 412

## *Introductory Nuclear Engineering*

### Exam 1 Review



# Chapter 1 - Fundamentals

- Nuclear units
- Elementary particles/particle physics
- Isotopic nomenclature
- Atomic weight/number density
- Chart of nuclides
- Mass energy equivalency



# Chapter 2 – Quantum Mechanics

- Special Relativity – time, length, mass changes
- Relativistic mass/momentum/energy relations
- Particle-wave duality
- Schrödinger's wave equation
- Heisenberg's uncertainty principle



# Chapter 3 – Nuclear Models

- Nuclear energy states
- Liquid Drop Model
- Nuclear mass equation
- Shell Model
- Nuclear stability
- Binding energy/mass excess
- Modern Nucleus concepts



# Chapter 4 – Nuclear Energetics

- Terminology
- Mass defect/BE
- Nuclear reactions
- Conserved quantities for various situations (not all the same!)
- **\*\*\*\*Q-Value\*\*\*\* (know how to calculate for ALL reactions)**
  - Know how to deal with charge
  - Know how to deal with excited nuclei
  - Know how to deal with electrons/binding energy of electrons



# Chapter 5 – Nuclear Decay

- Conservations
- Decay mechanisms – distinguishing features, Q values, energy/momentum balances
- \*\*\*Energy Diagrams\*\*\*
- Alpha/Beta particle energy distribution
- Decay Constant
- Half-Life
- Activity



# Chapter 5 – Nuclear Decay (cont)

- Parallel/Series Decay Routes
- Decay Chains
- Solutions to decay chain equations  
Secular Equilibrium
- Radionuclides in nature
- Carbon 14 dating
- Other isotopic dating methods
- Three component decays
- Isobars and most stable masses



# Chapter 6 – Binary Nuclear Reactions

- Definitions
- Types of binary reactions
- Reaction Mechanisms
- Kinematics (scattering example)
- Threshold Energy
- Neutron Reactions
- Neutron Scattering/slowness
- Neutron Energy Spectrums
- Lethargy





# Chapter 6 – Binary Nuclear Reactions (cont.)

- Neutron capture vs. slowing
- Fission reactions
- Emitted/recoverable fission energy
- Critical energies for fission
- Fertile vs. fissile vs. fissionable
- Fission product distribution
- Prompt vs. delayed neutrons
- Fission steps/timeline



# Chapter 7 – Radiation Interactions with matter

- Linear Interaction Coefficient (micro vs. macro)
- Cross section (micro vs. macro)
- Attenuation in Material
- Derivation of material interaction
- Buildup factor
- Mass Attenuation Coefficient
- Energy dependence of cross sections
- Cross section Trends



# Chapter 7 – Radiation Interactions with matter (cont.)

- Cross Section of mixture
- Total intensity/flux
- Neutron flux
- Time/space/position dependence of flux
- Fluence
- Uncollided flux transmission
- Thermal vs. fast neutrons
- Photon Interactions – types, trends, energies, cross sections
- Charged Particle interactions
- Stopping Power (collision vs. radiative)
- Range



# Example 1

$$N = \frac{\rho N_A}{A} e$$

$$95\% \text{ } ^{238}\text{U}$$

$$\phi = \frac{\text{neutrons}}{\text{cm}^2 \cdot \text{s}}$$

Assume a fuel rod has a diameter of 1 cm and a length of 5 m.

Assuming an enrichment of 5%  $^{235}\text{U}$  and a thermal flux of  $2 \times 10^{13}$  neutrons, what is the reaction rate in the fuel rod for:

- scattering?
- fission?

$$\Sigma_f \quad \boxed{\hat{R} = \sigma_f N \phi} \quad \frac{\text{reactions}}{\text{cm}^3 \cdot \text{s}}$$

$$\sigma_s = \sigma_t - \sigma_a - \sigma_f$$

$$\sigma_{s,235} = 13.76$$

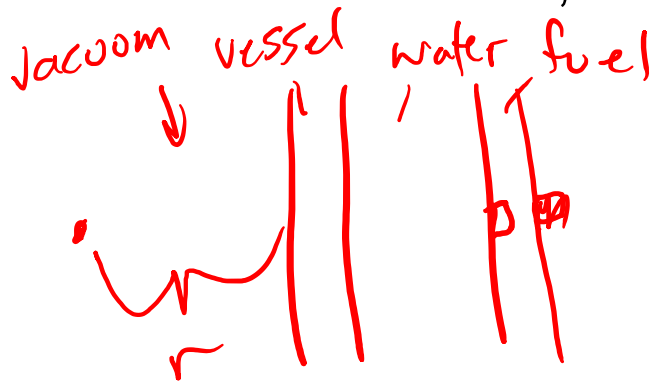
$$\sigma_{s,238} = 9.476$$

$$\hat{R}_s = \left[ (\sigma_s N)_{238} + (\sigma_s N)_{235} \right] \phi$$

reactions  
scatters  
s

# Example 2

In order to start up a fission reactor,  $1 \text{ cm}^3$  of this rod must reach a neutron flux of  $1 \times 10^{12} \text{ neutrons/cm}^2/\text{s}$ . Assuming that an isotropic neutron source is 1 meter away from the 4 cm thick iron reactor vessel, and that there is 8 cm of water between this rod and the vessel wall, what is the required source intensity to start this reactor? (Hint, use fission cross section, rather than the total for the  $^{235}\text{U}$ )



$$\phi = \frac{S_n}{4\pi r^2} (e^{-\Sigma_t \Delta x_w + \Sigma_f \Delta x_v})$$

$$R = \hat{R} \cdot V_d = \Sigma_f \cdot V_d \cdot \phi = \frac{S_n \Delta V_d \Sigma_{f,235}}{4\pi r^2} \left[ e^{-(\Sigma_t \Delta x)_w} - e^{-(\Sigma_t \Delta x)_v} \right]$$

# Example 3

- The Radionuclide  $^{41}\text{Ar}$  decays by  $\beta^-$  emission to an excited level of  $^{41}\text{K}$  that is 1.293 MeV above the ground state. What is the maximum kinetic energy of the emitted  $\beta^-$  particle?
- What makes this the maximum energy?



# Solution

## Q Equation

$$Q_{\beta^-} = \{M(^{41}_{18}\text{Ar}) - [M(^{41}_{19}\text{K}) + E^*/c^2]\}c^2$$

$$[40.9645008 - 40.9618259] \cdot 931.5 - 1.293 \text{ MeV}$$

$$= 1.199 \text{ MeV}$$

B) Because an antineutrino is also released, which carries away some energy – this maximum is when the antineutrino has zero energy



# Example 4

- What is the probability of producing  $^{91}\text{Br}$  in a fission reaction?
- Use fission product mass distribution chart:
- $\sim 8.5\%$





# Example 5

- What is the amount of thermal neutrons that are absorbed in water per  $\text{cm}^3$  over 1 hour in a fission reactor if the thermal flux is  $2.2 \times 10^{16}$  neutrons/ $\text{cm}^2/\text{s}$ ? ( $\Sigma_a = 0.0197 \text{ cm}^{-1}$ )
- $1.56 \times 10^{19}$  absorptions per  $\text{cm}^3$

