Chemical Engineering 412

Introductory Nuclear Engineering

Lecture 16 Nuclear Reactor Theory I Nuclear Criticality



Spiritual Thought

"Things will work out' may well be President Hinckley's most repeated assurance to family, friends, and associates. 'Keep trying' he will say. 'Be believing. Be happy. Don't get discouraged. Things will work out'"

Elder Jeffrey R. Holland



Graduate Student Visit Day



Tour research labs, talk with the faculty and staff, meet other students, visit with College of Graduate Studies. Lunch is included.

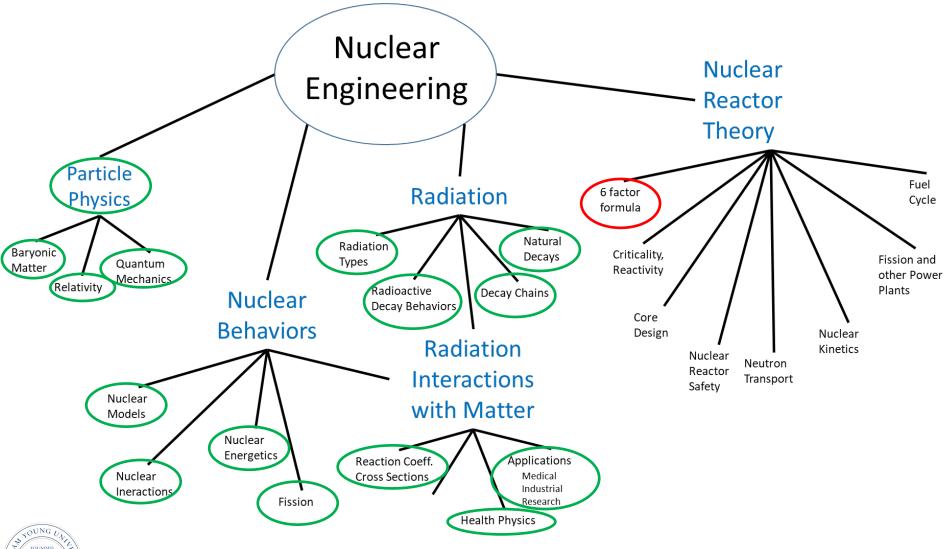
Idaho Falls Center

1784 Science Center Drive Thursday, March 28 10 a.m. - 4 p.m.



RSVP by March 20: Madeline at sticht@uidaho.edu

Roadmap





Objectives

- Know the 6 factor formula (+ each factor)
- Understand (memorize) terminology for nuclear reactors
- Know the 6 factor formula (+ each factor)
- Know differences between heterogeneous and homogeneous cores
- Know the 6 factor formula (+ each factor)
- Understand General trends of 6 factors



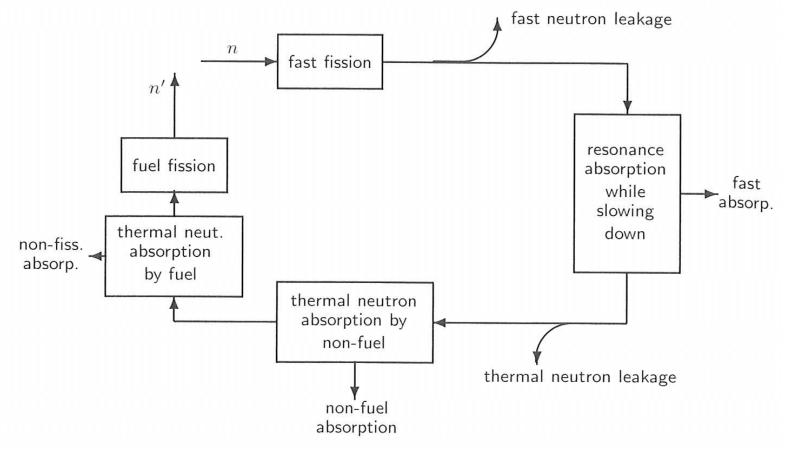
Core Nomenclature

- Fuel fissile material in core
- Heavy atoms generally fissile, fertile, and fissionable material
- Moderator collision material that slows neutrons
- Cladding fuel containment
- Reflector core wrapping that minimizes neutron leakage
- Blanket material used to produce useful isotopes from core
- Shielding neutron (and other radiation) absorbing material to protect personnel and instrumentation



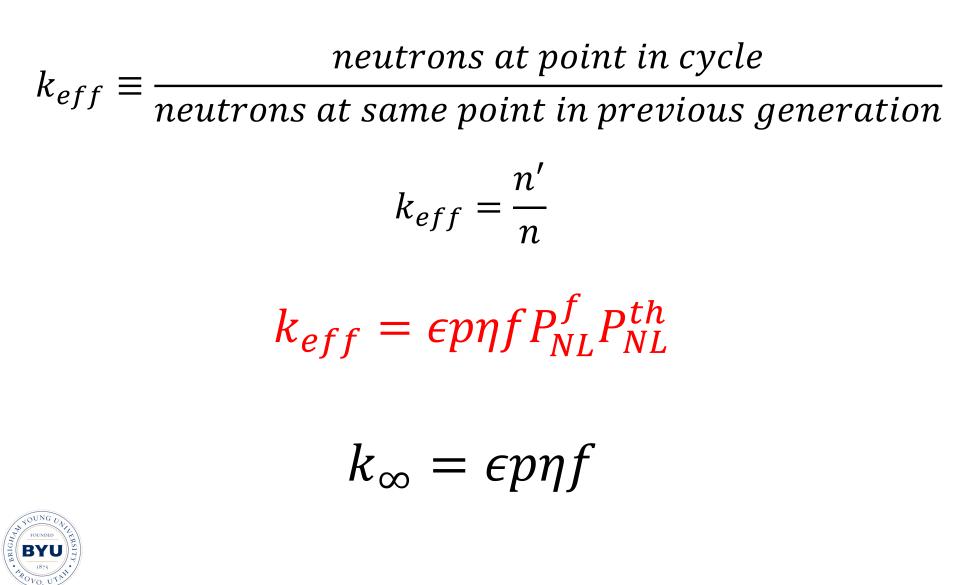
Fast Neutron Life Cycle

• What happens to fast neutrons?





Multiplication Factor



Reactor Considerations

• Increase Power?

$$k_{eff} > 1$$

• Decrease Power?

$$k_{eff} < 1$$

- Most reactors have K_{eff}>1, but cancel excess out with absorptive "poisons", which are removed with time.
- Most reactors designed to avoid prompt supercriticality
- If k_{eff} increases, "feedback" effects resist increase
- What if we want to change amount of fuel or moderator?
 - Impacts various "six factor" parameters
 - Changes k_{eff}



Fast Neutron Factors

- Fast Fission, ε
- Resonance Escape Probability, p
- thermal utilization, f
- Fission factor, η
- Fast non-leakage probability, P_{NL}^{f}
- Thermal non-leakage probability, P_{NL}^{th}
- Investigate for two reactor types:
 - Homogenous

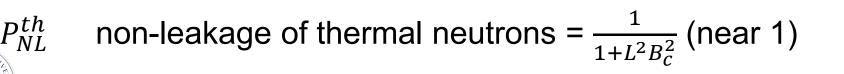


– Real (heterogeneous)

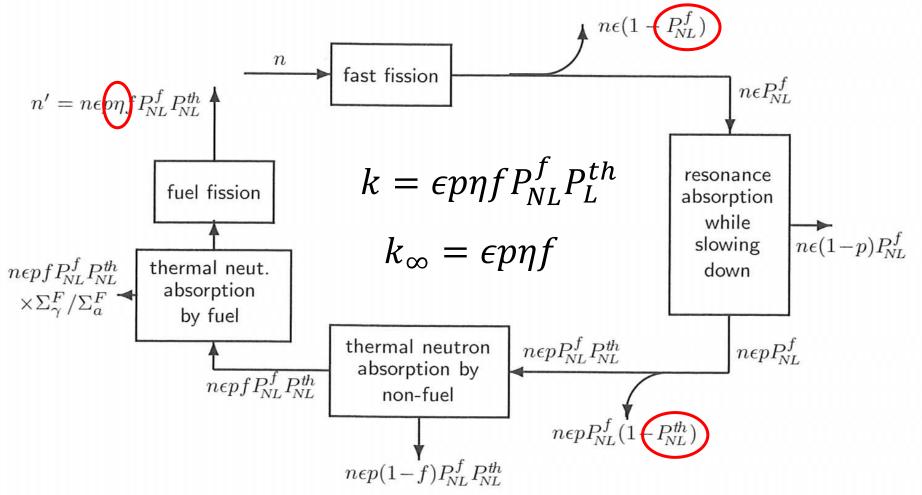
Six Factor Formula

$$n' \equiv n\epsilon p\eta f P_{NL}^f P_{NL}^{th}$$

- n' next generation neutrons
- *n* neutrons produced per thermal fission
- ϵ ratio of total neutrons to thermal neutrons (1.0-1.08)
- *p* resonance escape probability (0.8-0.9)
- $f \qquad \text{thermal utilization} = \frac{\Sigma_a^F \phi^F V^F}{\Sigma_a^F \phi^F V^F + \Sigma_a^{NF} \phi^{NF} V^{NF}} (0-1)$ $\eta \qquad \text{fission factor} = v \frac{\Sigma_f^F}{\Sigma_a^F} (2.0-2.2)$
- P_{NL}^{f} non-leakage of fast neutrons = $\exp(-B_{c}^{2}\tau)$ (near 1)



Quantitative Neutron Cycle





Moving forward: Assume a Homogenous Reactor

Thermal Fission Factor, η

For a homogenous reactor: $\phi_F = \phi_{NF}$

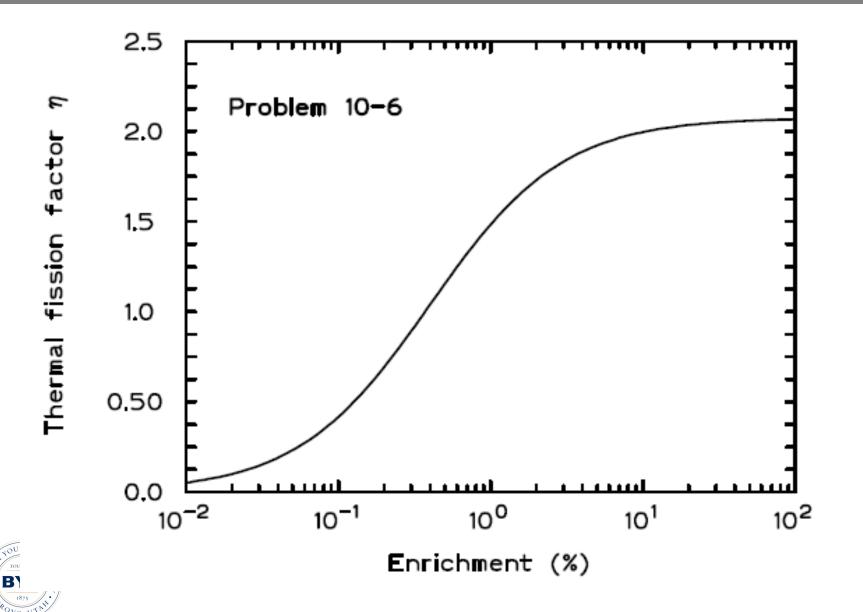
$$\eta \equiv v \frac{\Sigma_f}{\Sigma_a} = v \frac{\sigma_f^{235} N^{235}}{\sigma_a^{235} N^{235} + \sigma_a^{238} N^{238}} = \frac{v^{235} \sigma_f^{235}}{\sigma_a^{235} + \sigma_a^{238} \left(\frac{N^{238}}{N^{235}}\right)}$$

$$e = \frac{N^{235}}{N^{235} + N^{238}}$$
$$\Rightarrow \frac{N^{238}}{N^{238}} = \frac{1 - e}{e}$$

$$\eta = \frac{\nu^{235} \sigma_f^{235}}{\sigma_a^{235} + \sigma_a^{238} \left(\frac{1-e}{e}\right)}$$



η variation with fuel enrichment



Non-leakage probabilities

$$P_{NL}^{th} = \frac{1}{1 + L^2 B_c^2}$$

L thermal diff. length Σ_a absorption cross-sectionD thermal diff. coefficientf fuel utilization factor

$$L^{2} \equiv \frac{D}{\Sigma_{a}} = \frac{D^{M}}{\Sigma_{a}^{M}} \frac{\Sigma_{a}^{M}}{\Sigma_{a}^{M} + \Sigma_{a}^{F}} = L_{M}^{2} \left(1 - \frac{\Sigma_{a}^{F}}{\Sigma_{a}^{M} + \Sigma_{a}^{F}} \right) = L_{M}^{2} (1 - f)$$

- B_c critical buckling comes from reactor geometry
 - Table 10.6
 - Derived from Neutron Diffusion Equation
 - Balance of size and geometry of reactor



Conceptual Definitions

- $L = \frac{1}{2}$ distance thermal neutron travels from point of thermalization to absorption
- τ = 1/6 mean squared distance from initial (birth) point to thermalization point
- Neutrons
 - Travel further in fast spectrum
 - 30 vs. 6 cm in light water
 - Spend far more time as thermal neutrons
- Probability of non-leakage
 - Approaches 100% as reactor dimensions become infinite
 - Both fast and thermal neutrons.

Non-leakage probabilities

$$P_{NL}^f = \exp(-B_c^2 \tau)$$

 τ Fermi age

$\tau \approx \tau_M$

 B_c critical buckling – comes from reactor geometry (Table 10.6)



Bare Reactor Summary

