

Chemical Engineering 612

Reactor Design and Analysis

Lecture 15

Core Hydraulic Analysis

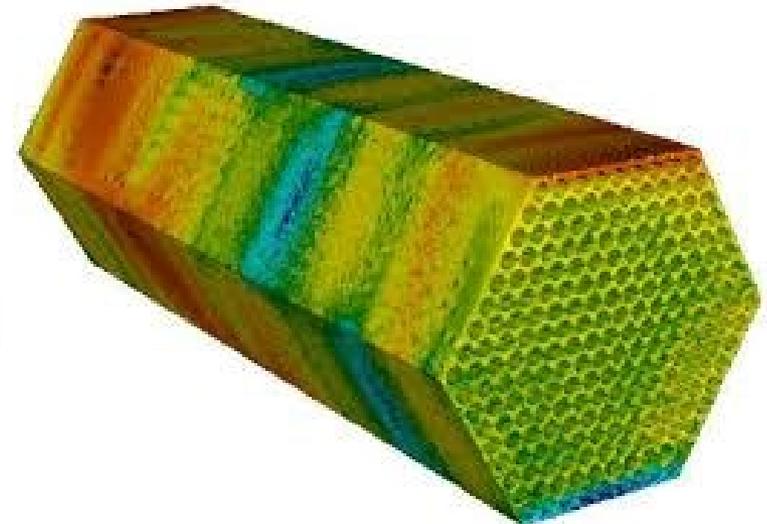
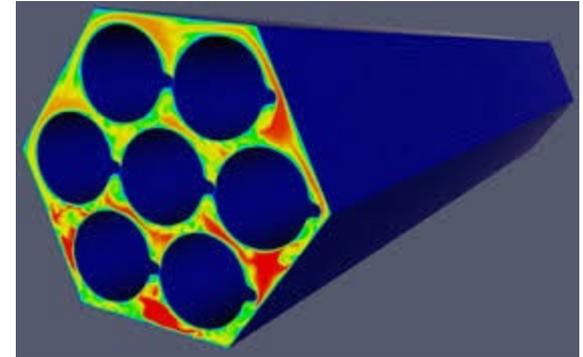


Spiritual Thought



Flow Analysis

- Size pumps
- Evaluate Erosion
- Flow rates for heat transfer
- Core sizing/dimensions
- Vibration analysis
- Core Orificing
- Valve/component sizing



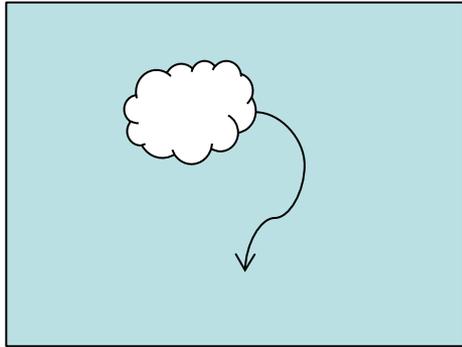
Flux

- Flux = quantity per unit area per unit time
 - Heat flux : $\text{J}/\text{m}^2 \cdot \text{s}$
 - Mass flux: $\text{kg}/\text{m}^2 \cdot \text{s}$
 - Neutron flux: $\text{neutrons}/\text{m}^2 \cdot \text{s}$
 - Momentum flux: $\text{kg} \cdot \text{m}/\text{s} \cdot \text{m}^2 \cdot \text{s} = \text{kg}/\text{ms}^2$
 - $\rho v = \text{kg}/\text{m}^3 * \text{m}/\text{s} = \text{kg}/\text{m}^2 \cdot \text{s} = \text{mass flux}$
- Then the flux of any quantity per unit mass (q) is
 - $\rho q v$
 - $q = h \rightarrow \text{J}/\text{m}^2 \cdot \text{s}$ Heat flux
 - $q = 1 \rightarrow \text{kg}/\text{m}^2 \cdot \text{s}$ Mass flux
 - $q = v \rightarrow \text{kg}/\text{s} \cdot \text{m}^2 \cdot \text{s} = \text{kg}/\text{m} \cdot \text{s}^2$ Momentum flux
- $-\rho * q * \mathbf{v} \cdot \mathbf{n} * A$ is the rate of quantity through surface A



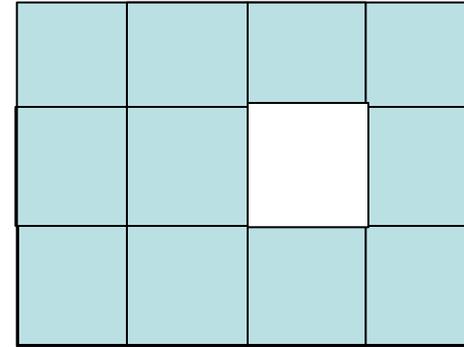
Lagrangian/Eulerian

Lagrangian



- Motion of system of **fixed mass**
- CONSERVATION LAWS
- Fluid elements move around and deform

Eulerian



- Some **fixed control volume**
- CONVENIENT FOR ENGINEERING
- Don't care about fluid elements
- Want pressure and velocity fields at a point.
 - Pressure on a wing
 - Drag on a car
 - Not the pressure of a chunk of fluid as it moves along

Differential Solution

- Differential Analysis
- Solution at any point in space
- Produce vector/scalar fields
 - Pressure
 - Velocity
 - Enthalpy
- CFD
- Common in Licensing, beyond class scope
- For concept reactors, use Eulerian approach



Integral Solution

- Utilize Reynolds Transport Theorem:

$$\frac{dB_{sys}}{dt} = \frac{d}{dt} \int_{CV} \rho b dV + \int_{CS} \rho b \vec{v} \cdot \vec{n} dA$$

- Recall that any property can be B_{sys}
 - Mass – Continuity Equation
 - Momentum – Force Vector Balance
 - Energy – Mechanical Energy Balance



Governing Equation

- $0 = \frac{d}{dt} \int_{CV} \rho dV + \int_{CS} \rho \vec{v} \cdot \vec{n} dA$
- $\sum \vec{F} = \frac{d}{dt} \int_{CV} \rho \vec{v} dV + \int_{CS} \rho \vec{v} \vec{v} \cdot \vec{n} dA$
- $\frac{dQ}{dt} + \frac{dW}{dt} = \frac{d}{dt} \int_{CV} \rho \left(u + \frac{1}{2} v^2 + gz \right) dV + \int_{CS} \rho \left(u + \frac{1}{2} v^2 + gz \right) \vec{v} \cdot \vec{n} dA$
- Combined, these give integral view of fluid dynamics, useful in reactor design



Mechanical Energy Equation

$$\downarrow$$

$$\frac{fLv^2}{2D}$$

- Can be viewed as multiple components of energy balance for control volume:
 - Gravity
 - Stagnation (acceleration)
 - Pressure difference
 - Friction
 - Shaft work

$$f_{\text{lam}} = 57/Re$$

$$\text{Colebrook} \quad \frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{2.51}{Re\sqrt{f}} \right)$$

$$\text{Haaland} \quad \frac{1}{\sqrt{f}} = -1.8 \log \left[\frac{6.9}{Re} + \left(\frac{\epsilon/D}{3.7} \right)^{1.11} \right]$$



Non-circular flow regions

- Non-circular flow

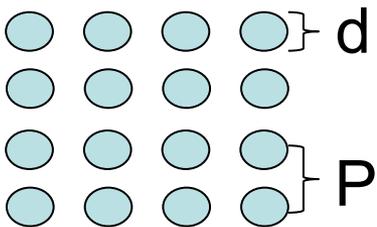
- Hydraulic Diameter, $D_e = \frac{4A}{P_w}$

- f_{lam} = shape specific

- $f_{\text{turb}} \sim$ round tube f



$$D_e = \frac{4A}{P_w} = \frac{4s^2}{4s} = s \quad f_{\text{lam}} = 57/Re$$



$$D_e = \frac{4A}{P_w} = \frac{4 \left(P - \frac{\pi}{4} D \right)}{\pi D} \quad f = \frac{C_{fL(\text{or } T)}}{Re^n}$$

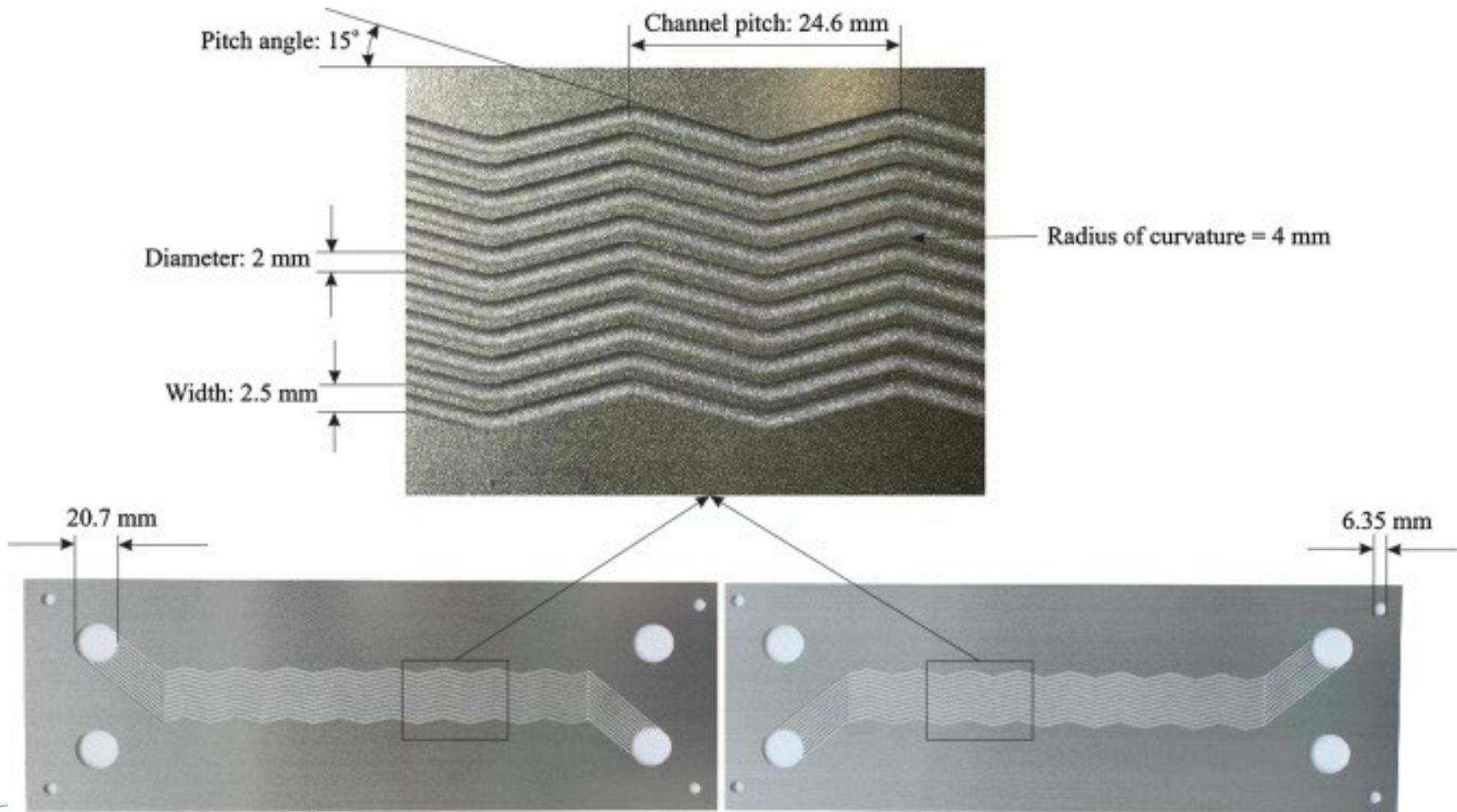
$n = 1$, laminar, $n = 0.18$, turbulent

Tube Bundle Friction

- Lam - $C_{fL} = a + b_1 \left(\frac{P}{D} - 1 \right) + b_2 \left(\frac{P}{D} - 1 \right)^2$
 - For edge and corners, P/D replaced by W/D
- Turb - $Re_{De} = 10^4 \rightarrow \frac{f}{f_{ct}} = 1.045 + 0.071 \left(\frac{P}{D} - 1 \right)$
- - $Re_{De} = 10^5 \rightarrow \frac{f}{f_{ct}} = 1.036 + 0.054 \left(\frac{P}{D} - 1 \right)$
 - OR $C_{fT} = a + b_1 \left(\frac{P}{D} - 1 \right) + b_2 \left(\frac{P}{D} - 1 \right)^2$
 - Coefficients found in Tables 9.5 and 9.6 of Nuclear Systems I
 - Add contributions from spacer grids and mixing vanes



PCHEs



Entrance Region Effects

- Velocity profile develops here
 - $\frac{z}{D_e} = 0.05Re$ (laminar)
 - $\frac{z}{D_e} = 25 - 40$ (turbulent)
- Characterized by higher f (flow acceleration)
- Exists for most flow disruptions Sensors far from orifices, obstructions, etc.



Flow Networks

- Pipe Networks composed of single pipes
- Pipes in series
 - Constant \dot{V} , additive ΔP
 - Type I – find ΔP
 - Type II – find \dot{V}
- Pipes in parallel
 - Constant ΔP , additive \dot{V}
 - Type I
 - Type II
 - Type III – Find D

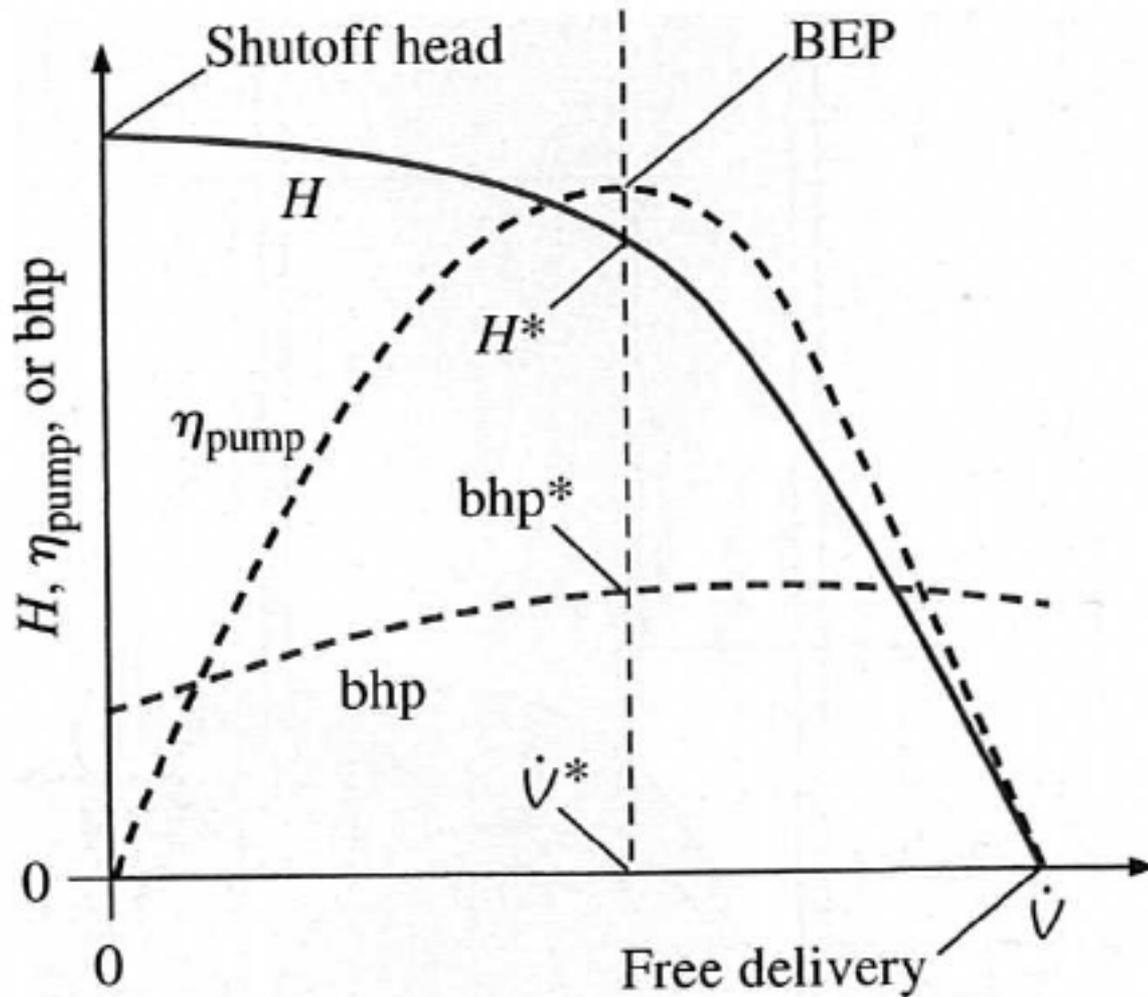


Sample Problem

- Calculate the pressure drop across a bare-rod core assembly (no spacer grids or mixing vanes) for a closed stainless steel square assembly with 264 tubes in square configuration, $P/D = 1.13$, $D = 0.34$ in, $L = 10$ ft, $S = 6.531$ in $\dot{m} = 100$ kg/s water.



Pump Curve Schematic



Pump Operation Curves

- Piping system requires a given \mathbf{V} and a given H .

$$H_{req} = \frac{P_2 - P_1}{\rho g} + \frac{v_2^2 - v_1^2}{2g} + (z_2 - z_1) + H_{loss}$$

- H_{loss} is friction and minor losses, etc.
- Pump has a corresponding \mathbf{V} and H .
- These **must match**, forming the operating point.
 - This may not be the best efficiency.
- Select a pump so that the best efficiency point (BEP) occurs at the operating point.
- Generally oversize the pump a bit
 - higher flow for given H_{req}
 - or Higher H_{avail} for given flow
 - Add a valve after pump \rightarrow raises H_{req} to match H_{avail} for given flow
 - Somewhat wasteful, but offers control.
 - Also may increase efficiency. (But higher efficiency may not compensate for extra work wasted in the valve (see example 14.2))

