

# Free Convection of Household Heater



Jedediah Alvey



# Free Convection

Objective: Determine how much heat is transferred from the side of the heater toward the other room due to free convection.

Assumptions:

- No forced convection, only free convection
- Constant, uniform surface temperature



# Free Convection

Dimensions/Constants:

$$T_s = 333 \text{ K } (140^\circ \text{ F})$$

$$T_\infty = 293 \text{ K } (68^\circ \text{ C})$$

$$\Rightarrow T_f = 313 \text{ K}$$

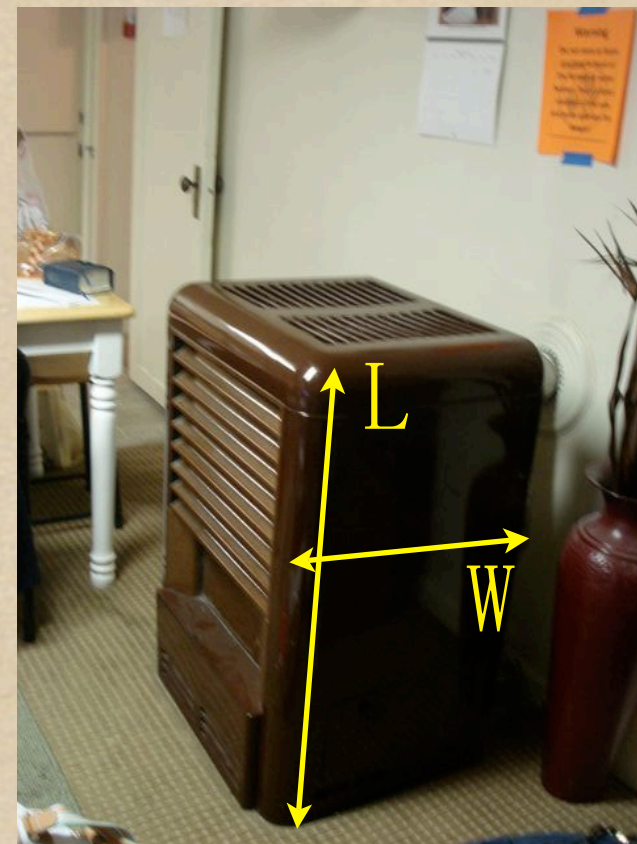
$$W = 0.33 \text{ m}$$

$$H = 0.80 \text{ m}$$

$$\nu = 17.2 \times 10^{-6} \text{ m}^2/\text{s}$$

$$\text{Pr} = 0.705$$

$$\beta = 1/T_f = 0.00319 \text{ K}^{-1}$$





# Free Convection

$$\begin{aligned} \text{Gr}_L &= (g \beta |T_s - T_\infty| L^3) / (\nu^2) \\ &= 2.17 \times 10^9 \end{aligned}$$

$$\begin{aligned} \text{Ra}_L &= \text{Gr}_L \cdot \text{Pr} \\ &= 2.17 \times 10^9 (.705) \\ &= 1.531 \times 10^9 \end{aligned}$$

⇒ Use eq. 9.26





# Free Convection

$$\text{Nu}_L = \{0.825 + (0.387\text{Ra}_L^{1/6}) / (1 + (0.492/\text{Pr})^{9/16})^{8/27}\}^2$$
$$= 140$$

$$\Rightarrow h = (K/L)\text{Nu}_L$$
$$= 4.78 \text{ W/m}^2\text{K}$$

and

$$q = h \cdot A (T_s - T_\infty)$$
$$= 4.78 (0.8 \times 0.33) (40)$$
$$= 50.5 \text{ Watts} \quad \leftarrow$$





# Comments

These results were from only considering free convection. Radiation would be a significant source of heat transfer as well, in comparison. Assuming  $\varepsilon = 0.5$ , heat transfer by radiation would be about 36.9 Watts.

From comparing Reynolds number to the Grashof number an induced wind speed of about 2 m/s (4.5 mph) would produce a significant source of heat transfer as well.