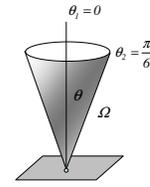
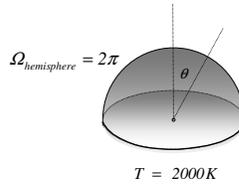
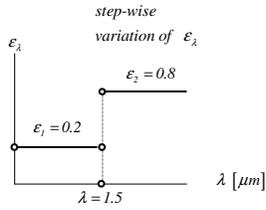
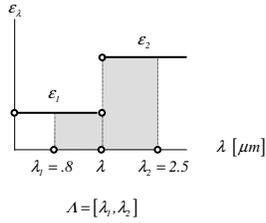


12.39 (7<sup>th</sup> Ed)



$$\Omega: \quad 0 \leq \theta \leq \frac{\pi}{6}$$

$$0 \leq \phi \leq 2\pi$$



**a**

$$\epsilon = \frac{E}{E_b} = \frac{\int_0^\infty E_\lambda d\lambda}{E_b} = \frac{\int_0^\infty \epsilon_\lambda E_{b\lambda} d\lambda}{E_b} = \epsilon_1 F_{0 \rightarrow \lambda=1.5}(T=2000\text{K}) + \epsilon_2 F_{\lambda=1.5 \rightarrow \infty}(T=2000\text{K}) = (0.2) \cdot (0.2732) + (0.8) \cdot (1 - 0.2732) = 0.636$$

**b**

$$E_{\lambda,\Omega} = \int_\Omega I_{\lambda,\theta} \cos\theta \, d\omega$$

$$= I_{\lambda,n} \int_\Omega \cos\theta \, d\omega$$

$$= I_{\lambda,n} \int_{\phi=0}^{2\pi} \int_{\theta=0}^{\pi/6} \cos\theta \sin\theta \, d\theta d\phi$$

$$= 2\pi I_{\lambda,n} \int_{\theta=0}^{\pi/6} \cos\theta \sin\theta \, d\theta$$

$$= 2\pi I_{\lambda,n} \int_{\theta=0}^{\pi/6} \sin\theta \, d[\sin\theta]$$

$$= 2\pi I_{\lambda,n} \left[ \frac{\sin^2\theta}{2} \right]_0^{\pi/6}$$

$$= \pi I_{\lambda,n} \left[ \frac{1}{4} - 0 \right]$$

$$= \frac{\pi I_{\lambda,n}}{4}$$

$$= \frac{E_\lambda}{4}$$

$$E_{\lambda,\Omega} = \int_A E_{\lambda,\Omega} d\lambda$$

$$= \int_{\lambda_1}^{\lambda_2} E_{\lambda,\Omega} d\lambda$$

$$= \frac{I}{4} \int_{\lambda_1}^{\lambda_2} E_\lambda d\lambda$$

$$= \frac{I}{4} \int_{\lambda_1}^{\lambda_2} \epsilon_\lambda E_{b\lambda} d\lambda$$

$$= \frac{I}{4} \left[ \int_{\lambda_1}^{\lambda} \epsilon_\lambda E_{b\lambda} d\lambda + \int_{\lambda}^{\lambda_2} \epsilon_\lambda E_{b\lambda} d\lambda \right]$$

$$= \frac{E_b}{4} \left[ \epsilon_1 \frac{\int_{\lambda_1}^{\lambda} E_{b\lambda} d\lambda}{E_b} + \epsilon_2 \frac{\int_{\lambda}^{\lambda_2} E_{b\lambda} d\lambda}{E_b} \right]$$

$$= \frac{E_b}{4} [\epsilon_1 F_{\lambda_1 \rightarrow \lambda} + \epsilon_2 F_{\lambda \rightarrow \lambda_2}]$$

$$= \frac{E_b}{4} [\epsilon_1 (F_{0 \rightarrow \lambda} - F_{0 \rightarrow \lambda_1}) + \epsilon_2 (F_{0 \rightarrow \lambda_2} - F_{0 \rightarrow \lambda})]$$

$$= \frac{\sigma T^4}{4} [\underbrace{\epsilon_1 (F_{0 \rightarrow \lambda} - F_{0 \rightarrow \lambda_1}) + \epsilon_2 (F_{0 \rightarrow \lambda_2} - F_{0 \rightarrow \lambda})}_{\epsilon_\lambda}]$$

$$= \frac{\sigma T^4}{4} (0.339)$$

$$= 76,900 \left[ \frac{\text{W}}{\text{m}^2} \right]$$