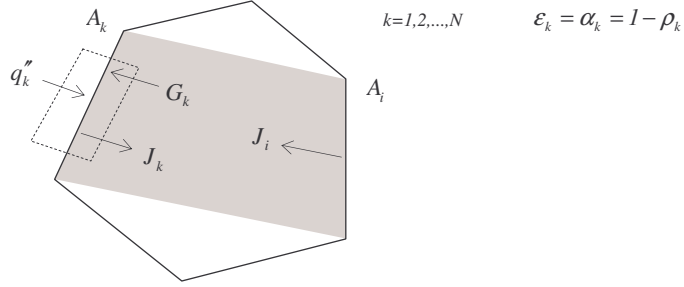


NET RADIATION METHOD FOR ANALYSIS OF RADIATION EXCHANGE IN DIFFUSE-GRAY ENCLOSURES

Consider an N -surface enclosure:



Net radiative flux at the surface k :

$$q_k'' = J_k - G_k \quad (1)$$

Radiosity of the surface k :

$$J_k = (1 - \epsilon_k) G_k + \epsilon_k E_{bk} \quad (2)$$

Consider definition of the view factor:

$$F_{ik} = \frac{q_{i \rightarrow k}}{q_i} = \frac{q_{i \rightarrow k}}{J_i A_i} \Rightarrow q_{i \rightarrow k} = J_i A_i F_{ik}$$

Then irradiation of the surface k

$$G_k = \frac{1}{A_k} \sum_{i=1}^N q_{i \rightarrow k} = \frac{1}{A_k} \sum_{i=1}^N J_i A_i F_{ik} = \frac{1}{A_k} \sum_{i=1}^N J_i A_i F_{ki} = \sum_{i=1}^N J_i F_{ki} \quad (3)$$

Substitute (3) into (1)

$$q_k'' = J_k - \sum_{i=1}^N J_i F_{ki} \quad (4)$$

Substitute (3) into (2)

$$J_k = (1 - \epsilon_k) \sum_{i=1}^N J_i F_{ki} + \epsilon_k E_{bk} \quad (5)$$

Solve (5) for $\sum_{i=1}^N J_i F_{ki}$

$$\sum_{i=1}^N J_i F_{ki} = \frac{J_k - \epsilon_k E_{bk}}{1 - \epsilon_k}$$

Substitute it into (4)

$$q_k'' = J_k - \frac{J_k - \epsilon_k E_{bk}}{1 - \epsilon_k}$$

it can be written also for surface i :

Then solve it for J_k

$$J_k = E_{bk} - \left(\frac{1}{\epsilon_k} - 1 \right) q_k'' \quad J_i = E_{bi} - \left(\frac{1}{\epsilon_i} - 1 \right) q_i'' \quad (6)$$

and substitute them into (4)

$$q_k'' = E_{bk} - \left(\frac{1}{\epsilon_k} - 1 \right) q_k'' - \sum_{i=1}^N \left[E_{bi} - \left(\frac{1}{\epsilon_i} - 1 \right) q_i'' \right] F_{ki}$$

note that $E_{bk} = E_{bk} \sum_{i=1}^N F_{ki} = \sum_{i=1}^N E_{bk} F_{ki}$

$$\begin{aligned} &= E_{bk} - \left(\frac{1}{\epsilon_k} - 1 \right) q_k'' - \sum_{i=1}^N E_{bi} F_{ki} + \sum_{i=1}^N \left(\frac{1}{\epsilon_i} - 1 \right) q_i'' F_{ki} \\ &= -\frac{q_k''}{\epsilon_k} + q_k'' + \sum_{i=1}^N (E_{bk} - E_{bi}) F_{ki} + \sum_{i=1}^N \left(\frac{1}{\epsilon_i} - 1 \right) q_i'' F_{ki} \end{aligned}$$

Then

$$\frac{q_k''}{\epsilon_k} - \sum_{i=1}^N F_{ki} \left(\frac{1}{\epsilon_i} - 1 \right) q_i'' = \sum_{i=1}^N F_{ki} (E_{bk} - E_{bi}) \quad k = 1, 2, \dots, N$$

$$\frac{q_k''}{\epsilon_k} - F_{k1} \left(\frac{1}{\epsilon_1} - 1 \right) q_1'' - F_{k2} \left(\frac{1}{\epsilon_2} - 1 \right) q_2'' - \dots - F_{kN} \left(\frac{1}{\epsilon_N} - 1 \right) q_N'' = F_{k1} (E_{bk} - E_{b1}) + F_{k2} (E_{bk} - E_{b2}) + \dots + F_{kN} (E_{bk} - E_{bN}) \quad (\text{NRM})$$